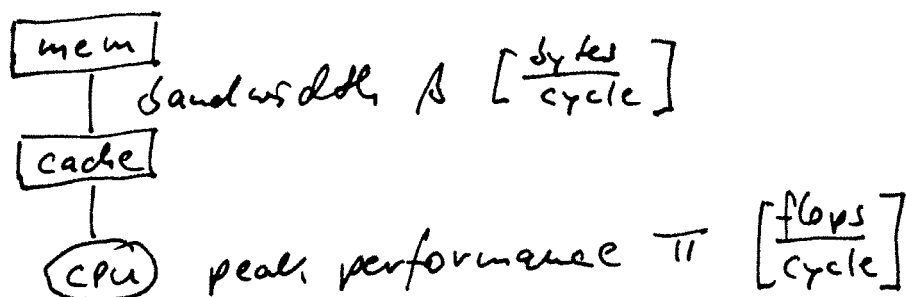


# Roofline Model

Goals:

- precise definition of compute/memory bound
- visualization and identification of optimization opportunities

Machine model:



Core 2:

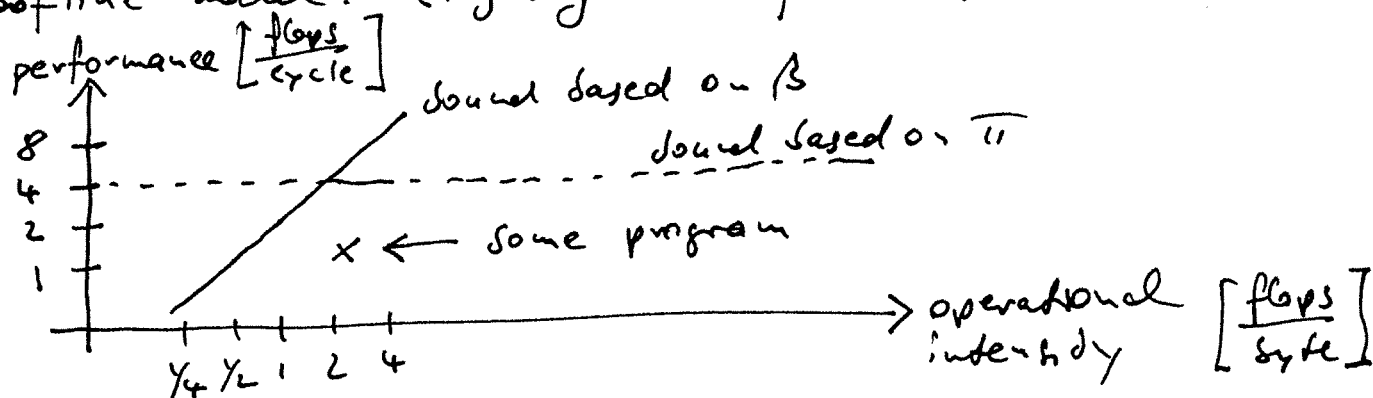
2

2 scalar }  
4 vec }

Program model:

operational intensity  $I = \frac{\# \text{ flops}}{\text{data} \leftrightarrow \text{mem}}$   $\left[ \frac{\text{flops}}{\text{byte}} \right]$

Roofline model: (log-log scale), example Core 2



bound based on  $\beta$ ?

assume a program has  $I = x$  flops/byte  
the program gets at most  $\beta$  bytes/cycle

$$\Rightarrow \text{performance} = y \leq \beta x$$

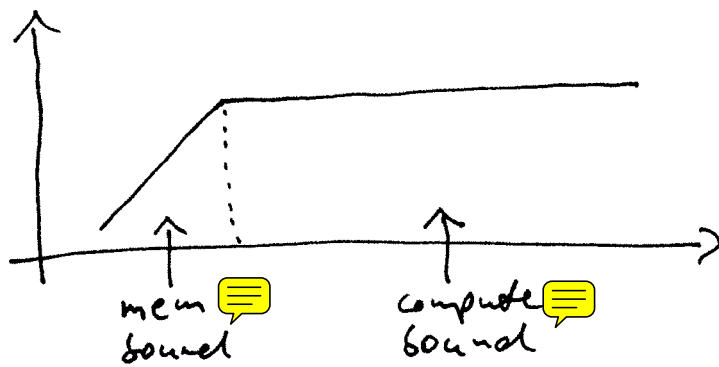
$$\log_2(y) \leq \log_2(x) + \log_2(\beta)$$

(line with slope 1)

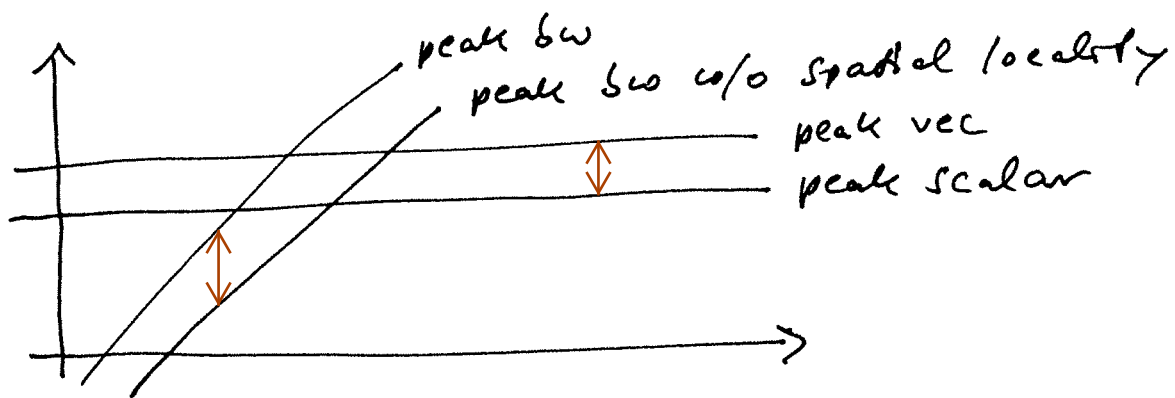
$$x=1 \Rightarrow y \leq \beta$$

What can you do with it?

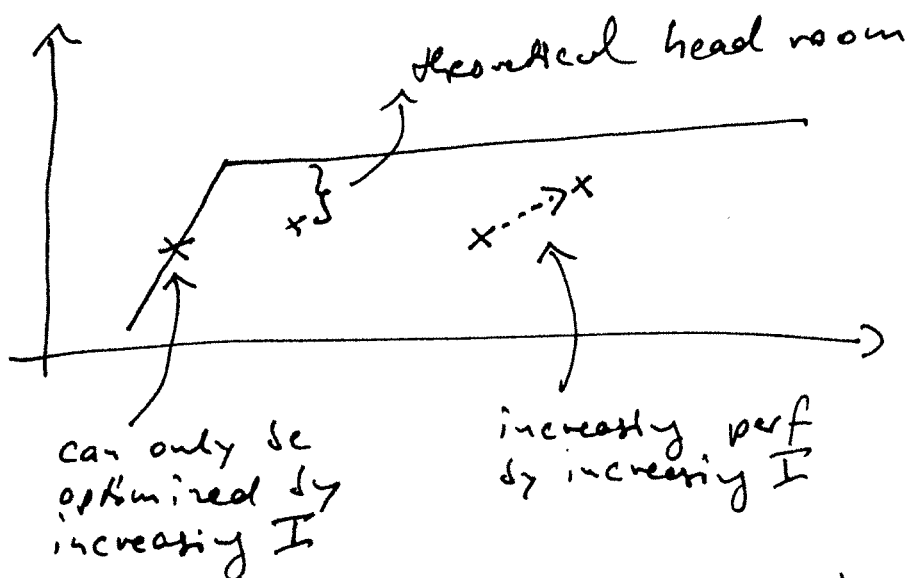
1.) memory/compute bound:



2.) more bounds



3.) program optimization



How to get roofline plot? Measure!