

POET: Parameterized Optimizations for Empirical Tuning

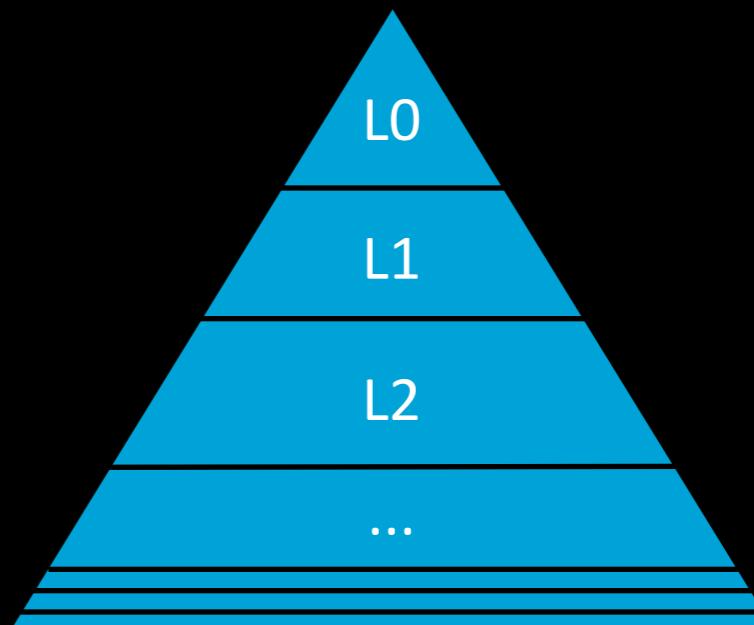
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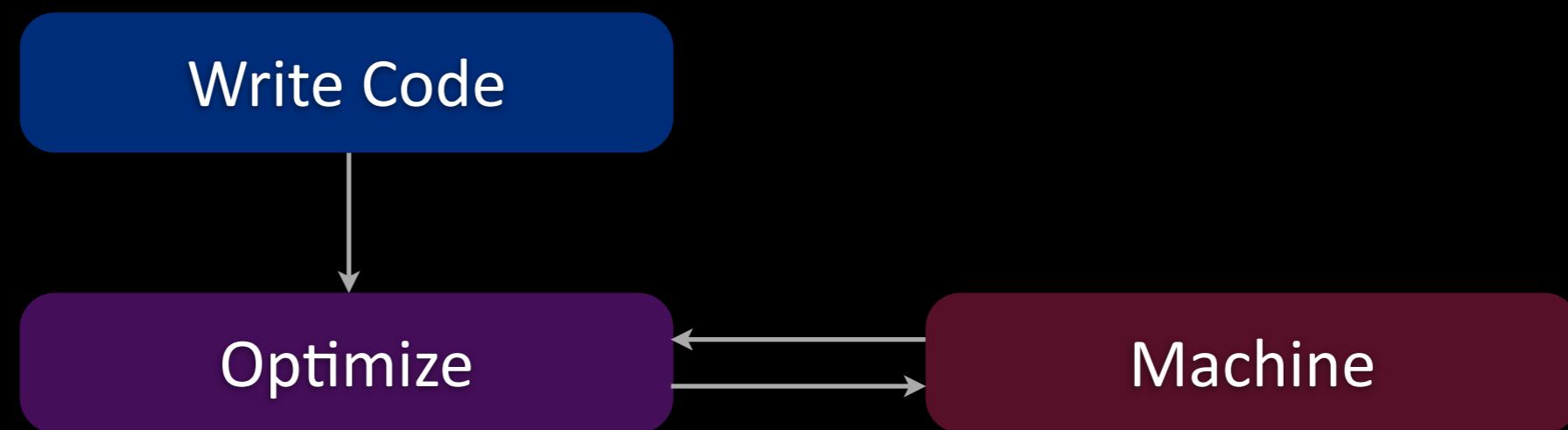
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Weibel Raphael, October 12th 2011



,<http://media.bestofmicro.com/parallelprocessing-multicore,9-P-58669-13.jpg>"

Empirical Tuning



PHiPAC

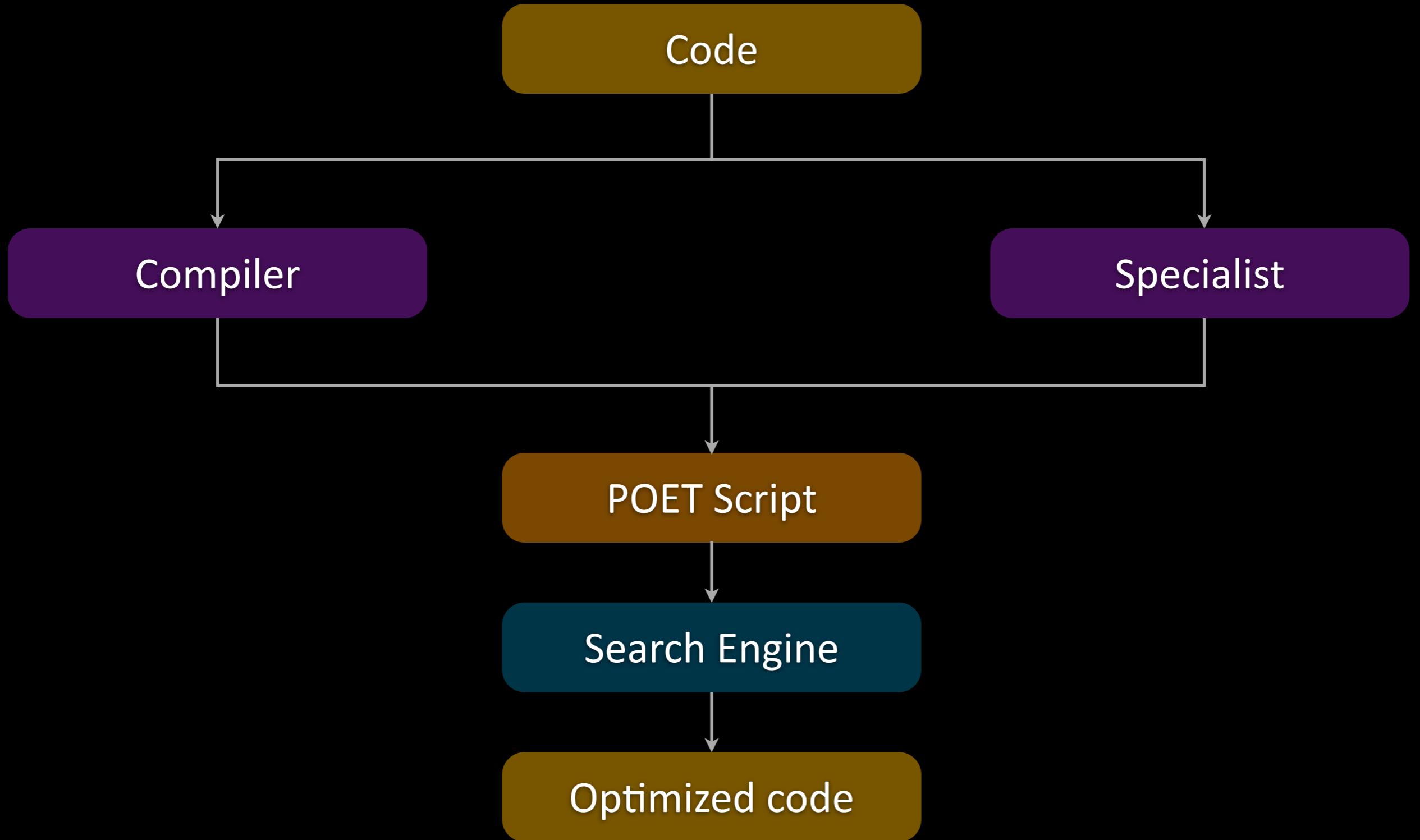
- BLAS Matrix-Matrix multiplication
- Code guidelines
- Empirical search for optimal loop parameters

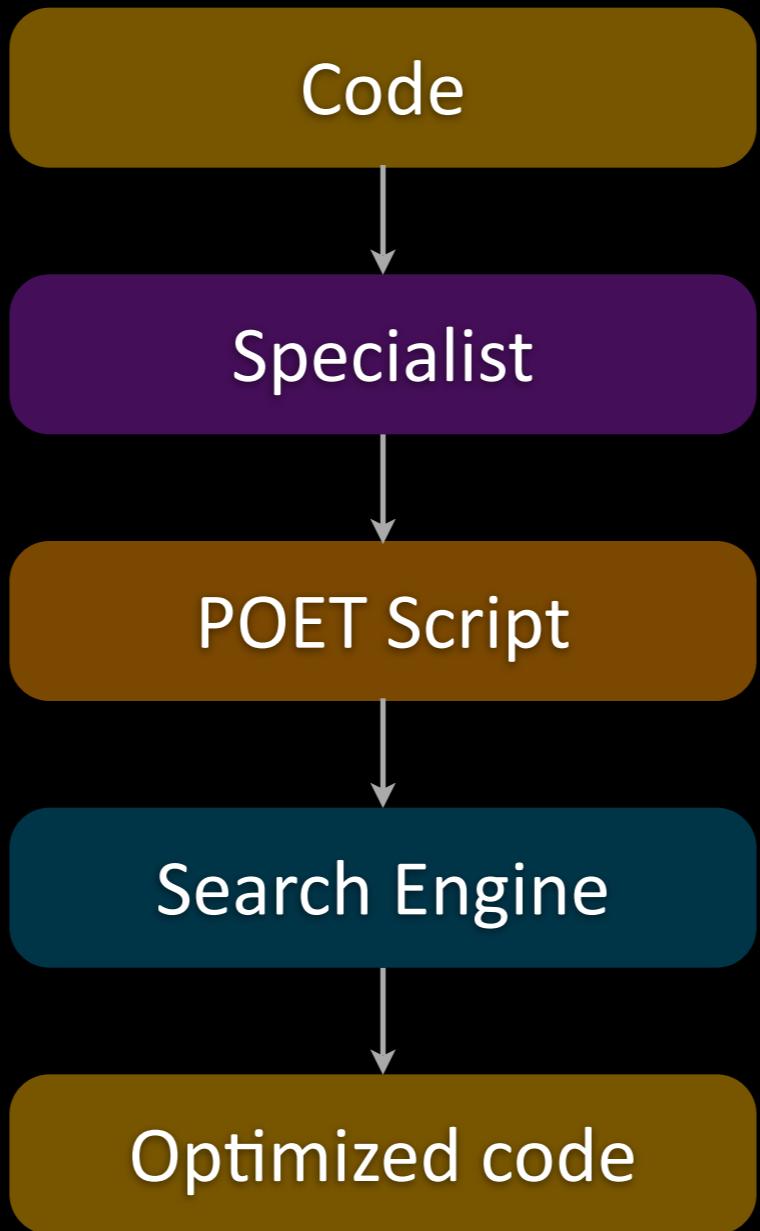
ATLAS

- For BLAS in general
- Automatic optimizations
- Empirical search of optimal code

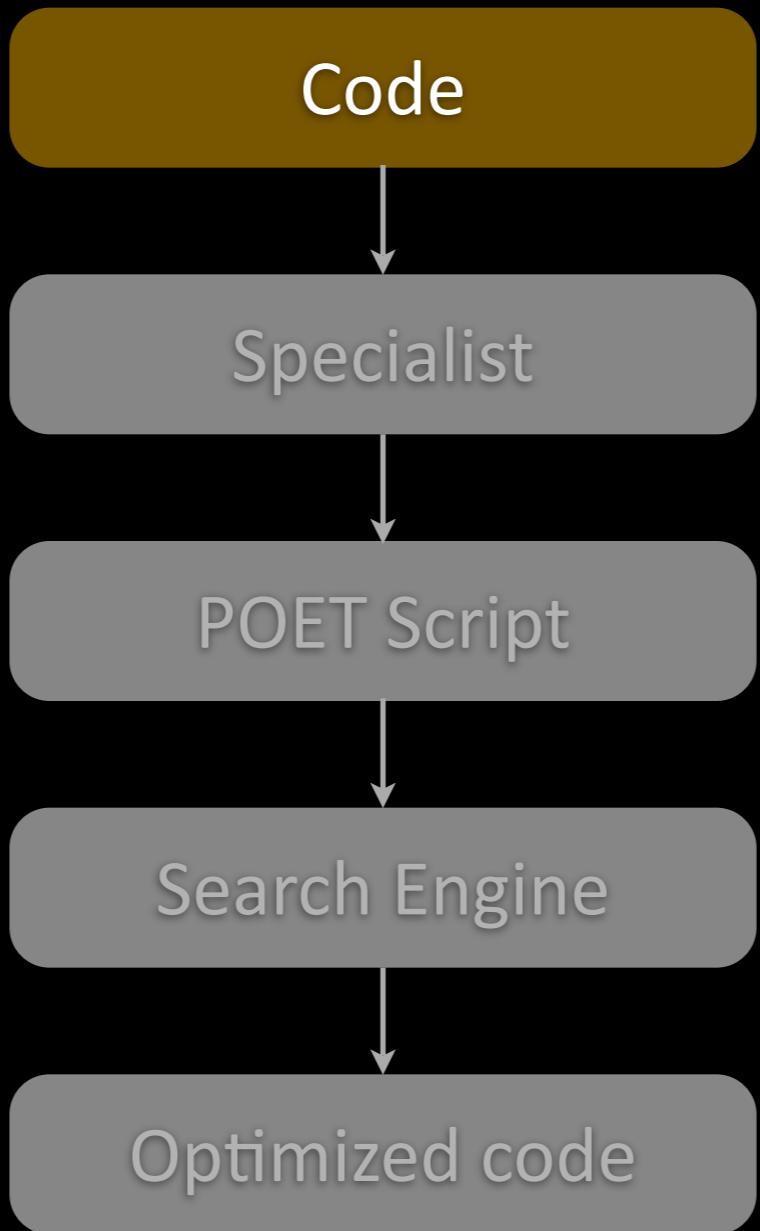
POET

„... parameterizing complex code transformations so that they can be empirically tuned.“

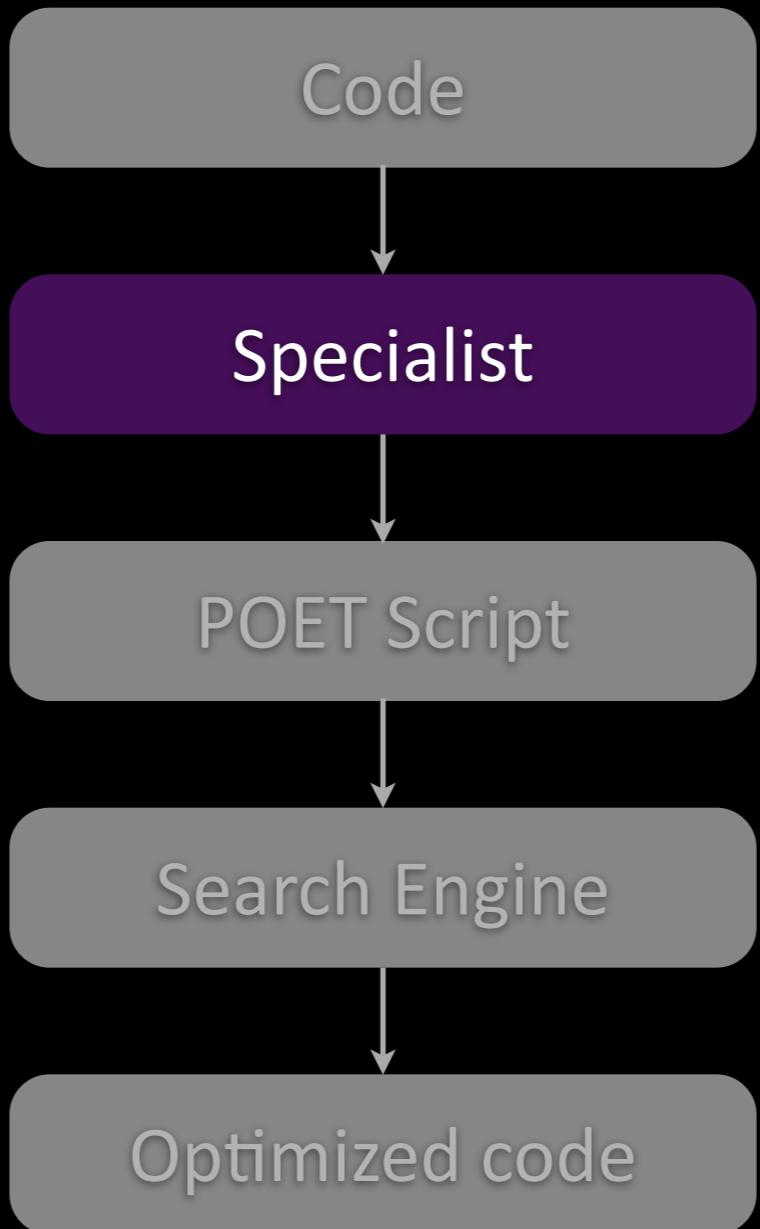


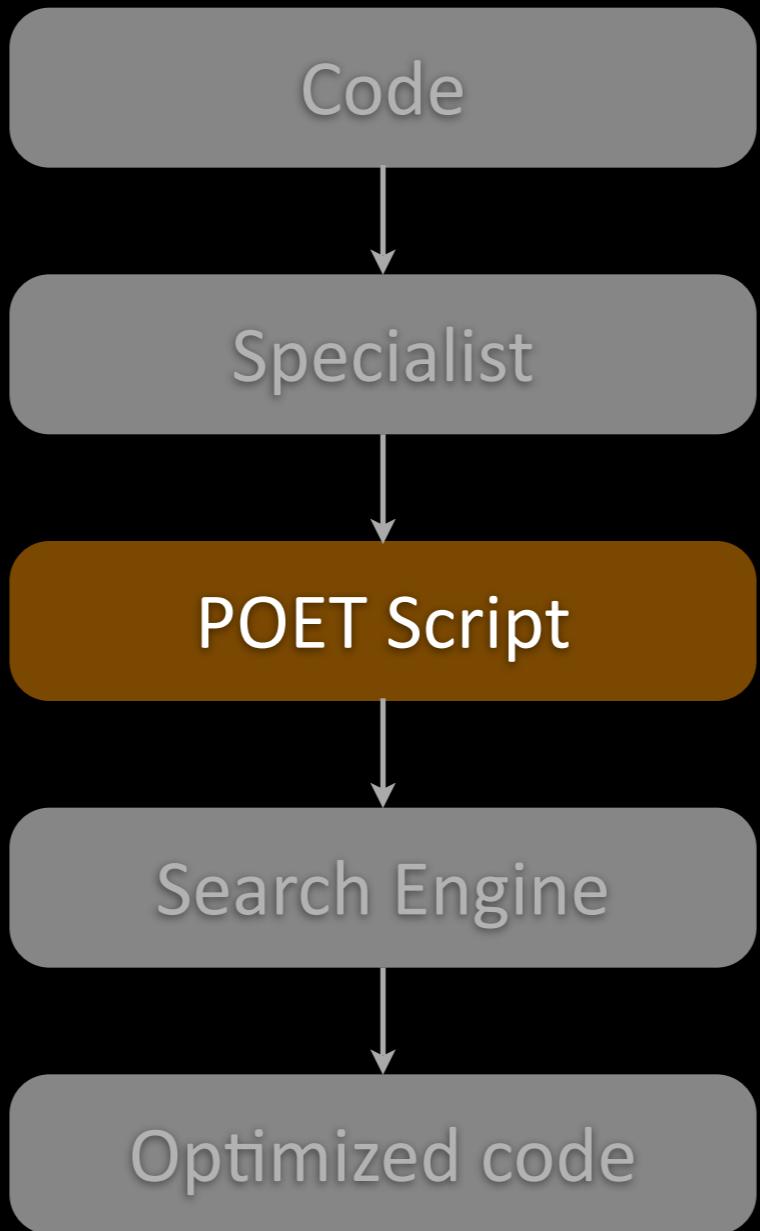


$$\underbrace{\begin{matrix} A \\ \hline L \end{matrix}}_{L} \times \underbrace{\begin{matrix} \text{Alpha} * B \\ \hline N \end{matrix}}_{N} = \underbrace{\begin{matrix} C \\ \hline N \end{matrix}}_{N} \quad M$$



```
void dgemm(int m, int n, int l, double alpha, double *a,double *b, double *c)
{
    for (i=0; i < m; i += 1) {
        for (j=0; j < n; j += 1) {
            for (k=0; k < l; k += 1) {
                c[i+j*m]+= alpha*b[k+j*l] * a[i+m*k];
            }
        }
    }
}
```





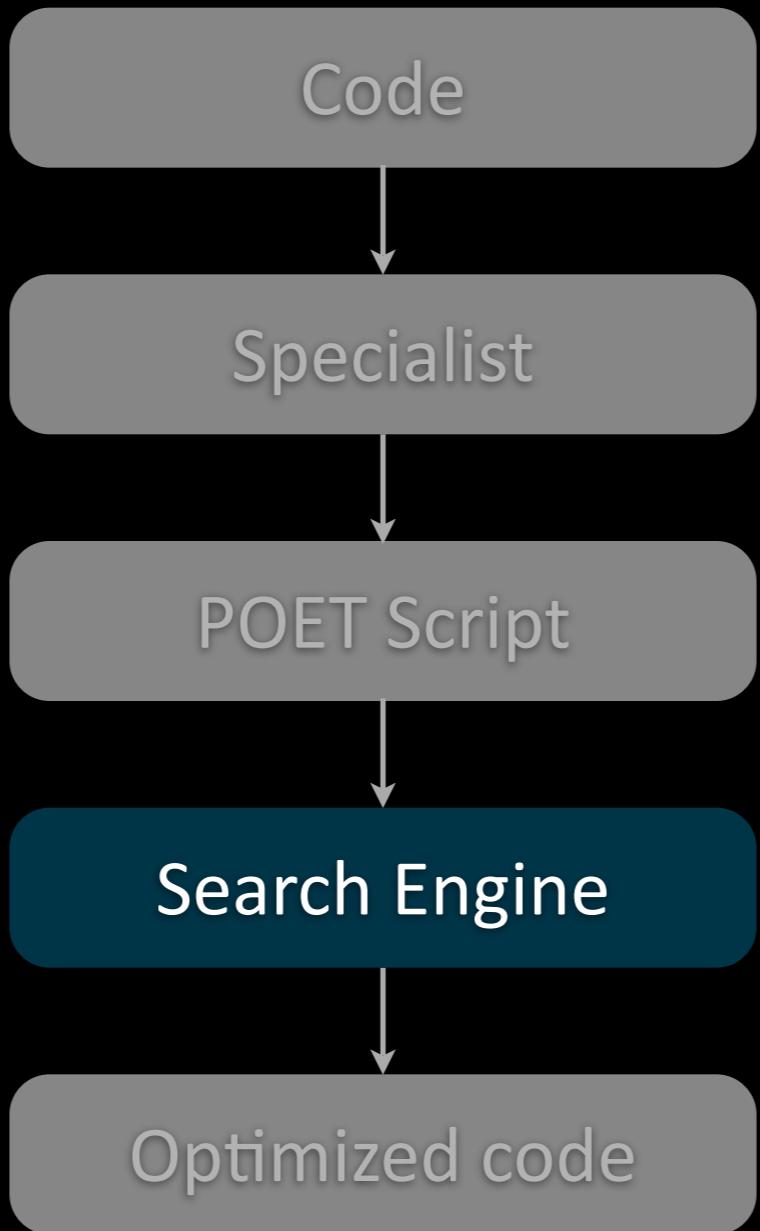
```
<code Loop pars=(i,start,stop,step) >
...
<xform Unroll pars=(input,uloop)...> ... </xform>
...

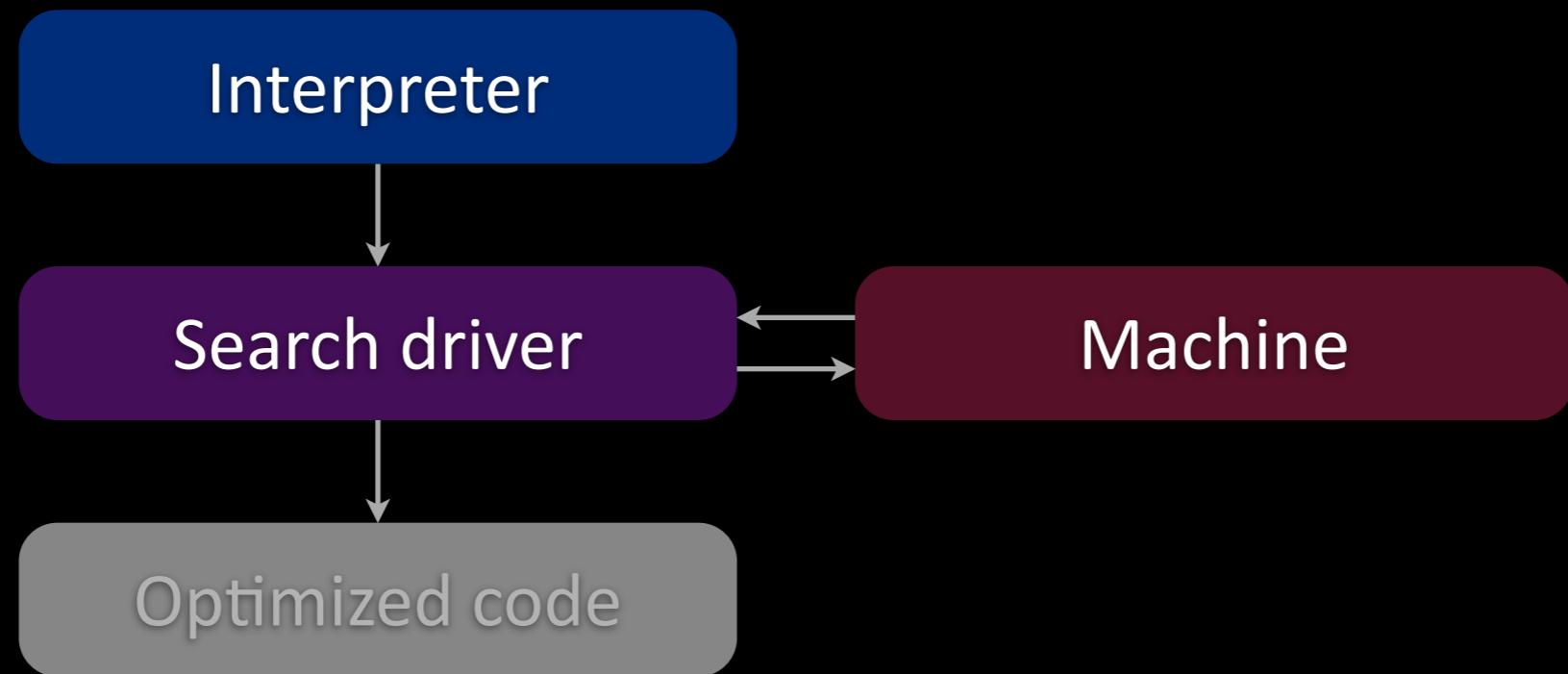
<define loopJ Loop#("j",0,"n",1)>
...

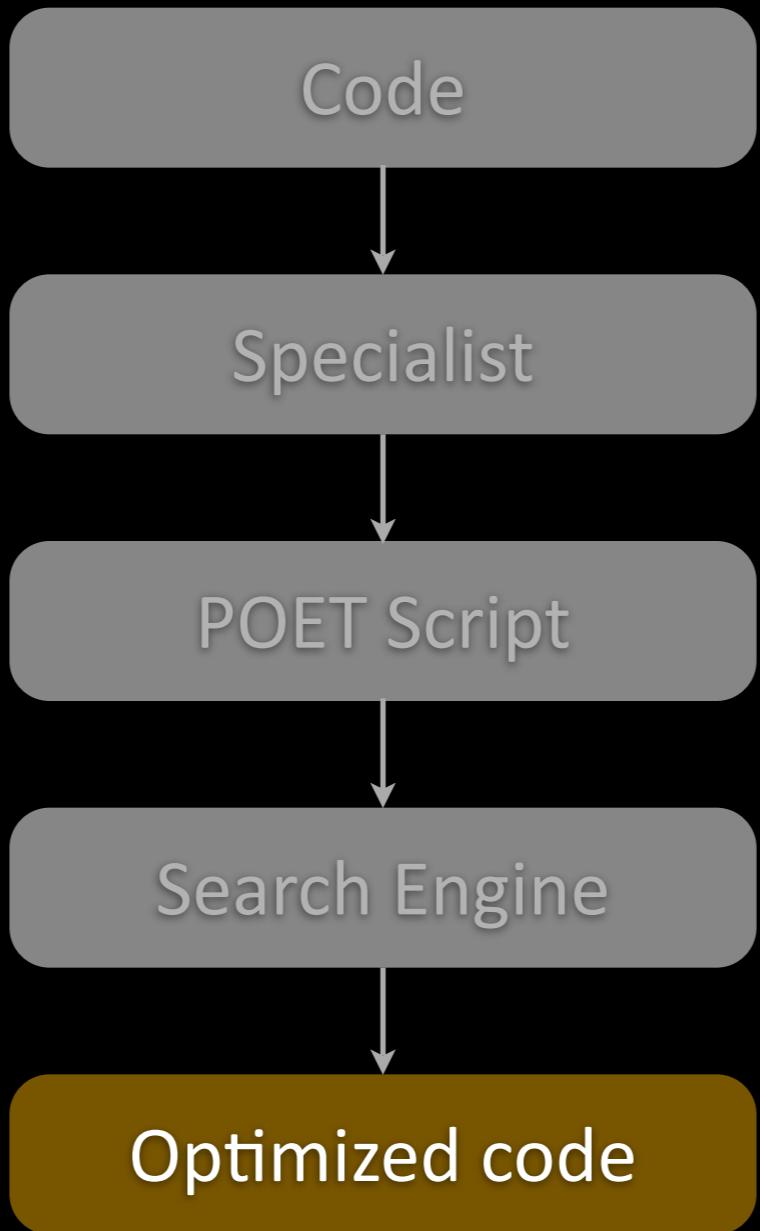
<define mmStmt "c[i+j*m]+= alpha*b[k+j*l] * a[i+m*k];">
<define nest1 Nest#(loopK,mmStmt)>
...

<define mmHead "void dgemm(int m, int n, int l, double alpha, double *a,
               double *b, double *c)">
<define dgemm Function#(mmHead, "int i, j, k;", nest3)>
<define mm_unroll (Unroll#(dgemm,loopK)) >
...

<output mm_unroll.c (Unroll.ur=8; mm_unroll)>
... 
```







```
void dgemm(int m, int n, int l, double alpha, double *a, double *b,
double *c)
{
    int i, j, k;
    int kk;
    for (i=0; i < m; i += 1) {
        for (j=0; j < n; j += 1) {
            for (k=0; k < l-7; k += 1) {
                c[i+j*m] += alpha*b[k+j*l] * a[i+m*k]; k+=1;
                c[i+j*m] += alpha*b[k+j*l] * a[i+m*k];
            } for ( ; k < l; k+=1) {
                c[i+j*m] += alpha*b[k+j*l] * a[i+m*k];
            }
        }
    }
}
```

POET Script

<code>

```
<code Loop pars=(i,start,stop,step) >

@init = (if start=="" then "" else (i "=" start ));
test = (if stop=="" then "" else (i "<=" stop ));
incr = (if step=="" then "" else (i "+=" step ));
@for (@init@; @test@; @incr@)

</code>
```

<xform>

```
<xform Unroll pars=(input,uloop) tune=(ur=16)>

if (!(input : Nest#(loop,body))) then (
    if (input : Function#(head,decl,body)) then
        Function#(head,decl,Unroll#(body,uloop))
    else if (input : Sequence#(s1,s2)) then
        Sequence#(Unroll#(s1,uloop),Unroll#(s2,uloop))
    else input
)

else if (loop != uloop) then
    Nest#(loop, Unroll#(body,uloop))
else if (!ur || ur == 1) then input
else (
    loop : Loop#(ivar,start,stop,step);
    dup = (body DUPLICATE#(_ , ur-1,(ivar "+=1;" ENDL body)));
    Sequence#(Nest#(Loop#(ivar,start,(stop "-" ur-1),step),dup),
    Nest#(Loop#(ivar,"",stop,step),body))
)

</xform>
```

<define>

```
<define loopJ Loop#("j",0,"n",1)>
<define loopI Loop#("i",0,"m",1)>
<define loopK Loop#("k",0,"l",1)>
<define mmStmt "c[i+j*m] += alpha*b[k+j*l] * a[i+m*k];">
<define nest1 Nest#(loopK,mmStmt)>
<define nest2 Nest#(loopI,nest1)>
<define nest3 Nest#(loopJ,nest2)>
<define mmHead "void dgemm(int m, int n, int l, double alpha, double *a,
                  double *b, double *c)">
<define dgemm Function#(mmHead, "int i, j, k;", nest3)>
<define mm_unroll (Unroll#(dgemm,loopK)) >
<define mm_block (Block#(dgemm,nest3,mmStmt))>
<define mm_permute (Permute#(dgemm,nest3,mmStmt))>
<define mm_block_unroll (Unroll#(mm_block, InnermostLoop#(mm_block)))>
```

<output>

```
<output mm.c dgemm>
<output mm_unroll.c (Unroll.ur=8; mm_unroll)>
<output mm_block.c (Block.bsize=(8 64 128); mm_block)>
<output mm_permute.c (Permute.order=(3 2 1); mm_permute)>
<output mm_block_unroll.c (Block.bsize=(16 16 8);Unroll.ur=8; mm_block_unroll)>
```

Formal Grammer

Sections

```
section :  
  "<" "code" ID {codeAttr} ">" Exp "<" "/code" ">"  
  | "<" "xform" ID {xformAttr} ">" Exp "<" "/xform" ">"  
  | "<" "define" ID Exp ">"  
  | "<" "output" FNAME Exp ">"
```

```

(1) poet : {section}
(2) section :
    "<" "code" ID {codeAttr} ">" Exp "<" "/code" ">"
(3) | "<" "xform" ID {xformAttr} ">" Exp "<" "/xform" ">"
(4) | "<" "define" ID Exp ">"
(5) | "<" "output" FNAME Exp ">"
(6) codeAttr : "pars" "=" "(" ID {"." ID} ")"
(7) xformAttr : "pars" "=" "(" ID {"." ID} ")"
(8) | "tune" "=" "(" ID "=" INT {"." INT} ";" ID "=" INT {"." INT} ")" )
(9) Exp : Op
    | Op ";" Exp | Op "," Exp | Op Exp
(10) Op : "if" Op "then" Op "else" Op (11) | ID {"." ID} "=" Op
(11) | ID ":" Op
(12) | ID {"." ID} "#" Unit | [ "car", "cdr", INT ] "#" Op
(13) | REPLACE "#" "(" Op "," Op "," Op ")"
(14) | PERMUTE "#" "(" Op "," Op ")"
(15) | DUPLICATE "#" "(" Op "," Op "," Op ")"
(16) | Op [ "+", "-", "*" ] Op | "-" Op
(17) | Op [ "<", "<=", ">", ">=", "==" , "!=" ] Op (18) | "!" Op | Op "&&" Op | Op "||" Op
(18) | Unit
(21) Unit : ID {"." ID} | INT | SOURCE | "(" Exp ")"

```

ID identifiers, e.g. Loop, Nest;
 FNAME file names, e.g., mm.c, ../dgemm.c;
 INT integer literals, e.g., 1, 0, 16, 64;
 SOURCE strings of code fragments;

Evaluation rules

DUPLICATE#

```
e := dup(lv,t,e1) for(i=0;i<t;++i)
    {set value(lv,i); e.val = list(eval(e1), e.val)}
```

```
<xform Unroll pars=(input,uloop) tune=(ur=16)>
    ...
    dup = (body DUPLICATE#(_,
        ur-1,(ivar "+=1;" ENDL body)));
    ...
</xform>
```

```

(1) e:=i           e.val = i.val
(2) | s           e.val = s.val
(3) | e1 e2       e.val = list(eval(e1), eval(e2))
(4) | e1 ,e2 ,...,em e.val = tuple(eval(e1),eval(e2), ..., eval(em))
(5) | car # e1   t = eval(e1); e.val = is list(t)?first(t) : t
(6) | cdr # e1   t = eval(e1); e.val = is list(t)?rest(t) : ""
(7) | i#e1        t = eval(e1); e.val = tuple elem(t,i.val)
(8) | cv#e1       if(!replaceCode) e.val = cv#eval(e1)
                  else {set pars(cv, eval(e1 )); e.val = eval(find_code(cv))}

(9) | e1 : e2     e.val = match_AST(e1,e2)
(10)| dv          e.val = find_code(dv)
(11)| lv          e.val = find_value(lv)
(12)| lv = e1     set_value(lv, eval(e1)); e.val = ""
(13)| xv # e1     set pars(xv, eval(e1)); e.val = eval(find_code(xv))
(14)| repl(e1 ,e2 ,e3 ) e.val = Replace(eval(e1), eval(e2), eval(e3))
(15)| perm(e1,e2) e.val = Permute(eval(e1), eval(e2))
(16)| dup(lv,t,e1) for(i=0;i<t;++i)
                  {set_value(lv,i); e.val = list(eval(e1), e.val)}

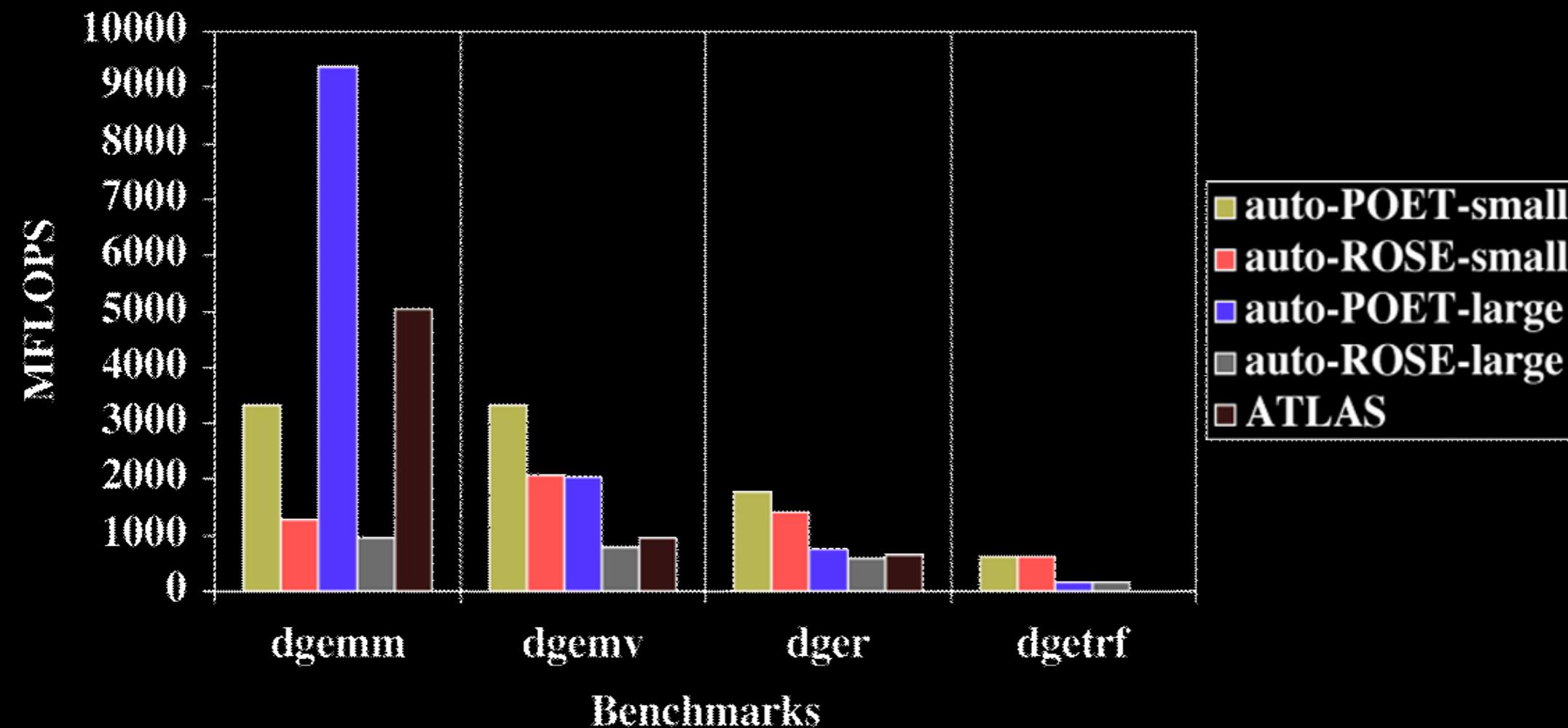
(17)| e1 ;e2      eval(e1): e.val = eval(e2 )
(18)| if(e1 ,e2 ,e3 ) e.val = bool(eval(e1))? eval(e2) : eval(e3)
(19)| e1 opi e2   e.val = eval(e1)opi e2 .val
(20)| ! e1        e.val = ! bool(e1.val)
(21)| e1 opb e2   e.val = bool(e1.val) opb bool(e2.val)

```

i: integer constants;
 s:string constants;
 lv: local variables;
 cv: global handles of code sections;
 dv: global handles of define sections;
 xv: global handles of xform sections;
 opi: integer binary operations (+,-,*,<,>,==,<=,>=,!);
 opb: boolean binary operations (&&, ||).

Results

AMD quad-core machine



Conclusion

- Supports any code transformation
- Supports all programming languages
- Supports Multi-Core CPU Architecture
- Does only optimize on the source code level

Further information

- <http://bigbend.cs.utsa.edu/poet/index.php>