



Computational Photography and Video: High-Dynamic Range Imaging

Prof. Marc Pollefeys

Dr. Gabriel Brostow

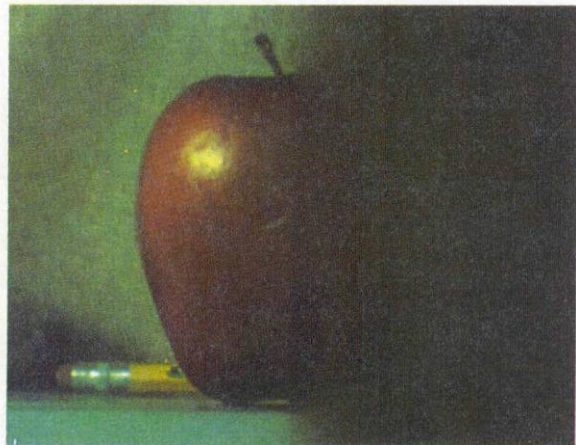
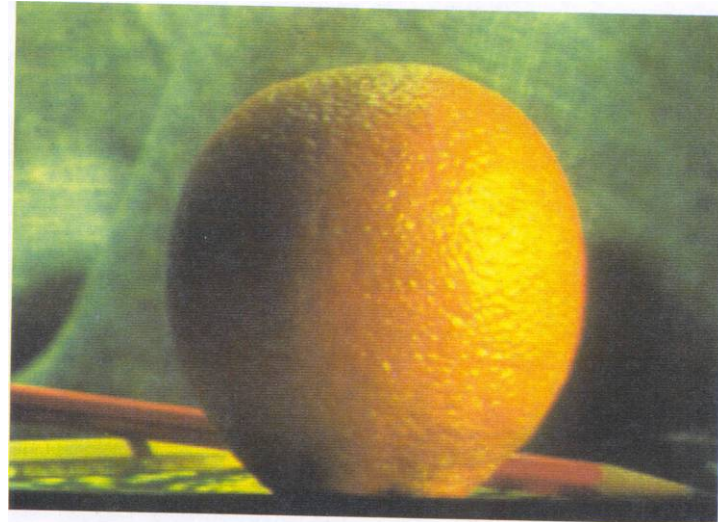
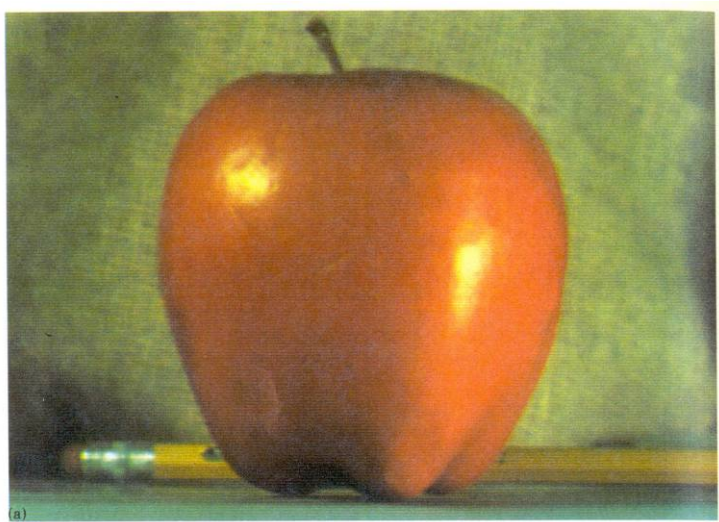
Today's schedule

- Last week's recap
- High Dynamic Range Imaging (LDR->HDR)
- Tone mapping (HDR->LDR display)

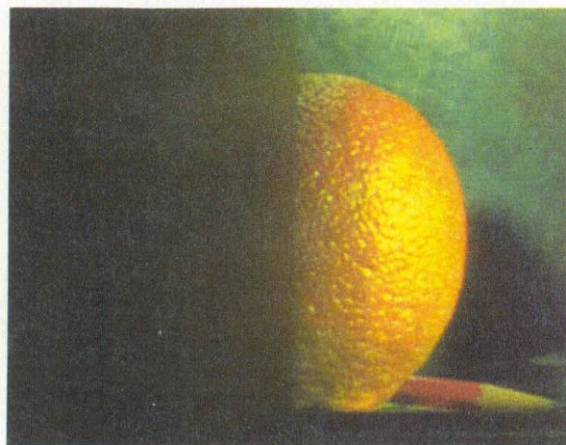
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Pyramid Blending



(d)

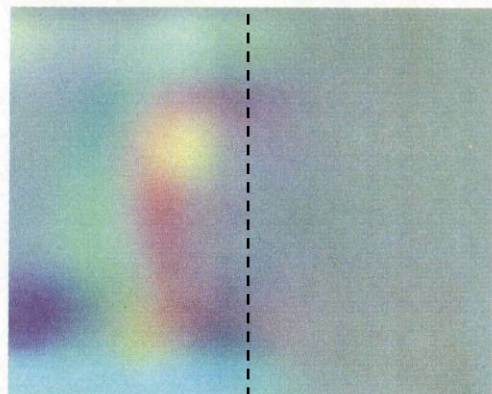


(h)

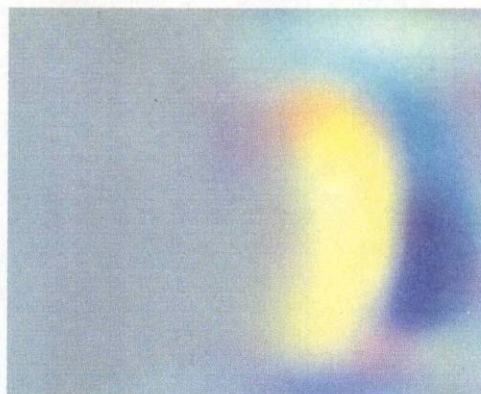


(l)

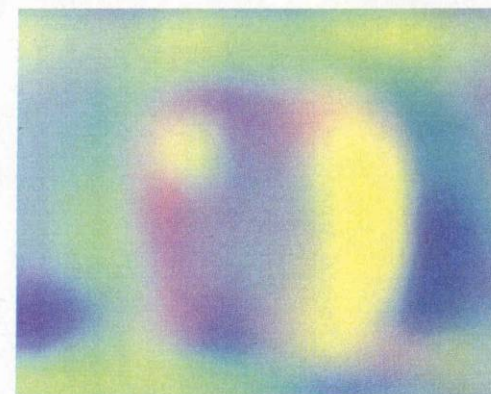
laplacian
level
4



(c)

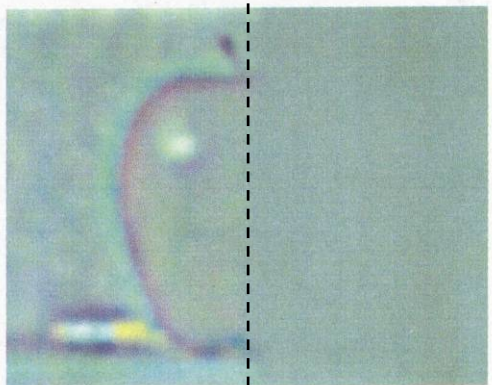


(g)

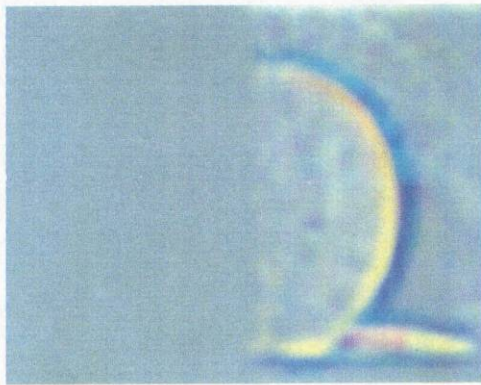


(k)

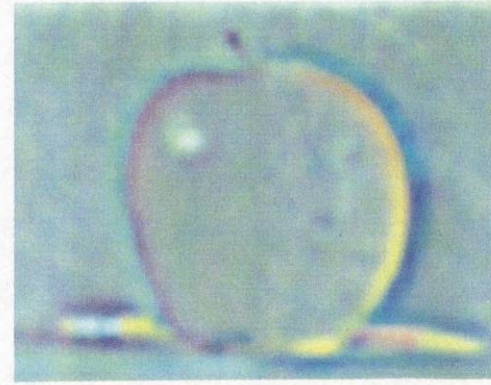
laplacian
level
2



(b)

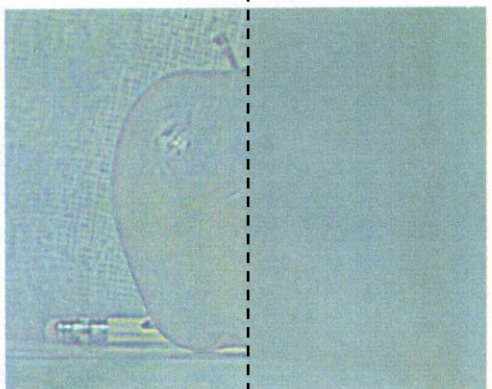


(f)

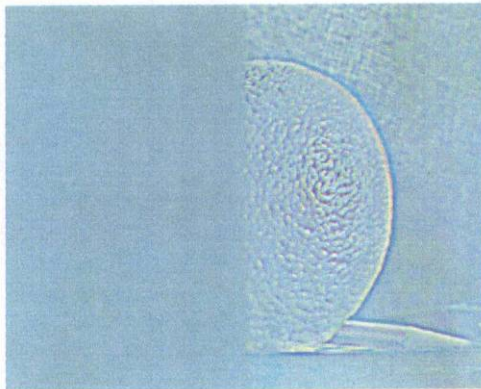


(j)

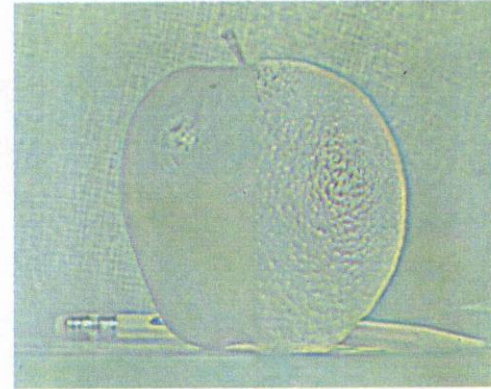
laplacian
level
0



(a)



(e)



(i)

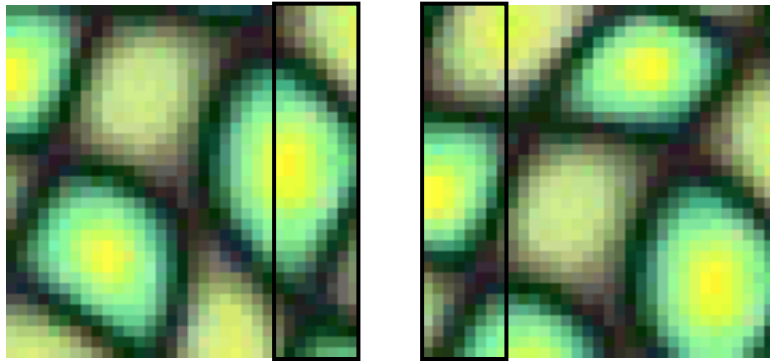
left pyramid

right pyramid

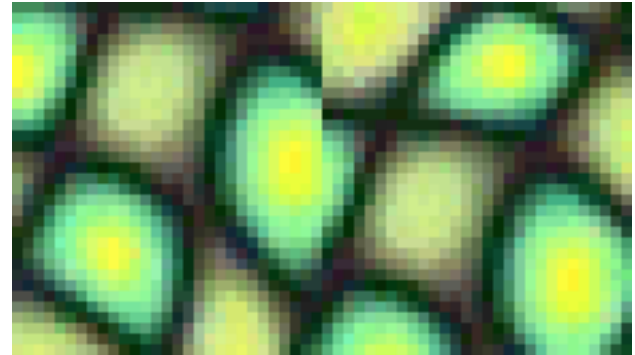
blended pyramid

Minimal error boundary

overlapping blocks

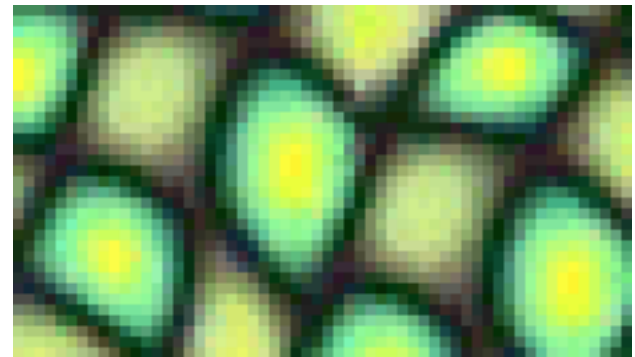


vertical boundary



A diagram illustrating the calculation of overlap error. It shows two overlapping blocks of the cell image. A large bracket encloses the overlapping region, with a minus sign between the two blocks and a superscript 2. This is followed by an equals sign and a small image showing a red line tracing the boundary of the overlapping region.

overlap error



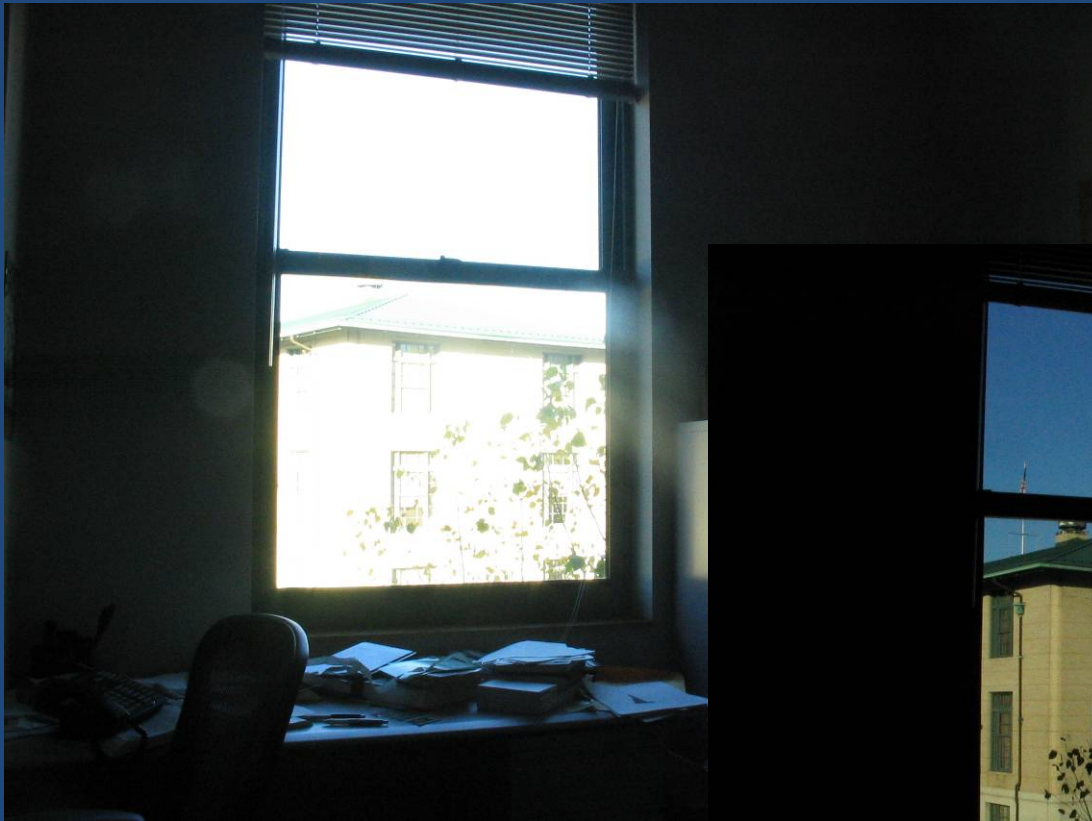
min. error boundary

Schedule	Computational Photography and Video	
20 Feb	Introduction to Computational Photography	
27 Feb	More on Cameras, Sensors and Color	Assignment 1: Color
5 Mar	Warping, morphing and mosaics	Assignment 2: Alignment
12 Mar	Image pyramids, Graphcuts	Assignment 3: Blending
19 Mar	Dynamic Range, HDR imaging, tone mapping	Assignment 4: HDR
26 Mar	<i>Easter holiday – no classes</i>	
2 Apr	TBD	Project proposals
9 Apr	TBD	Papers
16 Apr	TBD	Papers
23 Apr	TBD	Papers
30 Apr	TBD	Project update
7 May	TBD	Papers
14 May	TBD	Papers
21 May	TBD	Papers
28 May	TBD	Final project presentation

Today's schedule

- Last week's recap
- High Dynamic Range Imaging (LDR->HDR)
- Tone mapping (HDR->LDR display)

The Problem



Problem: Dynamic Range



1



1500



25,000



400,000

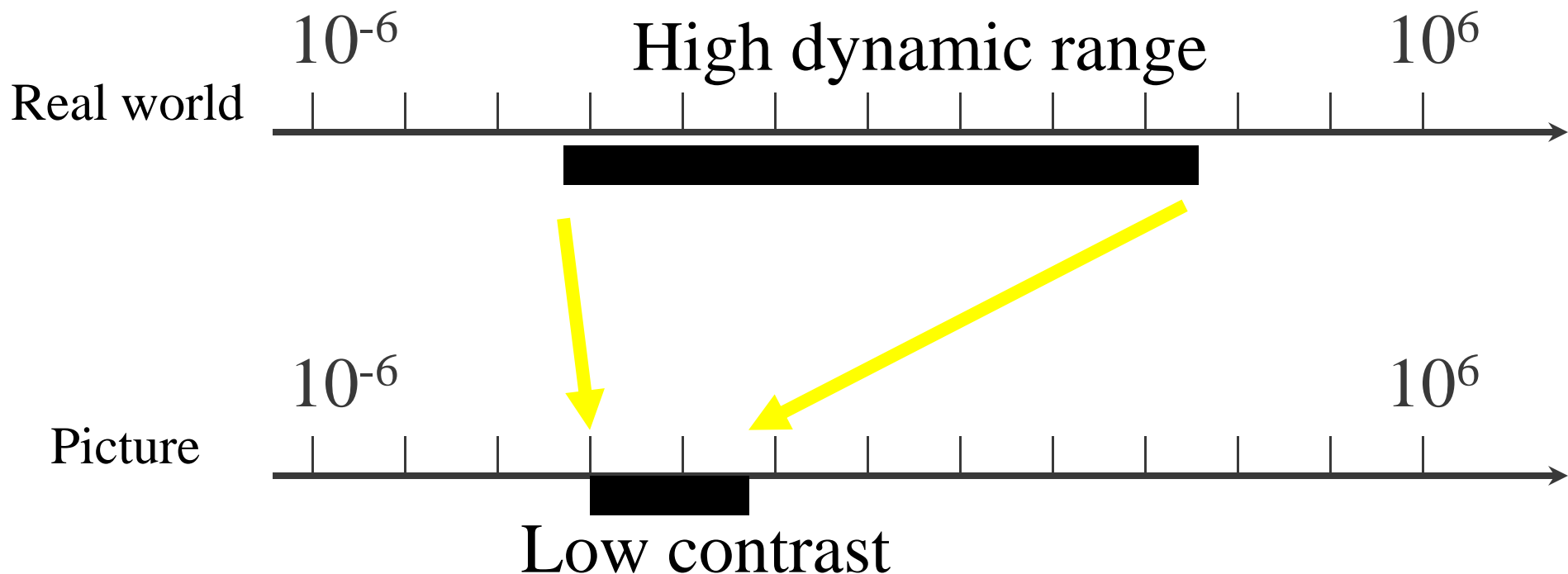


2,000,000,000

The real world is high dynamic range.

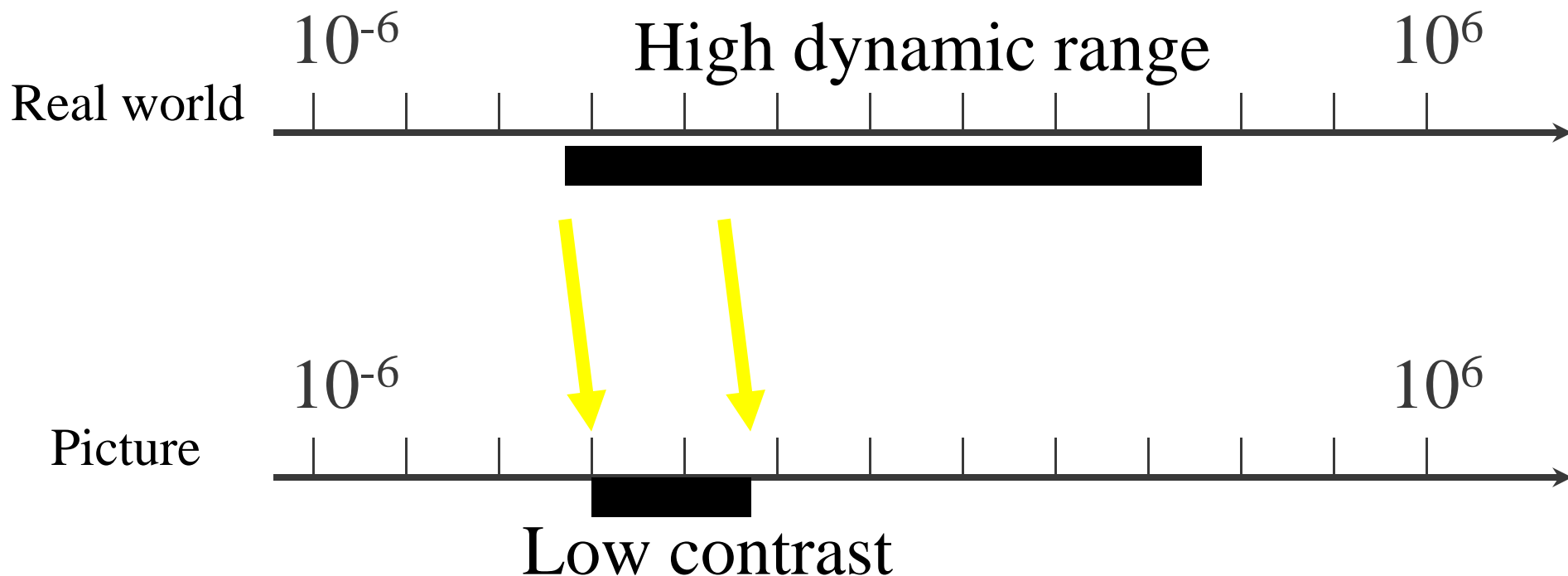
Multiple exposure photography

- Sequentially measure all segments of the range



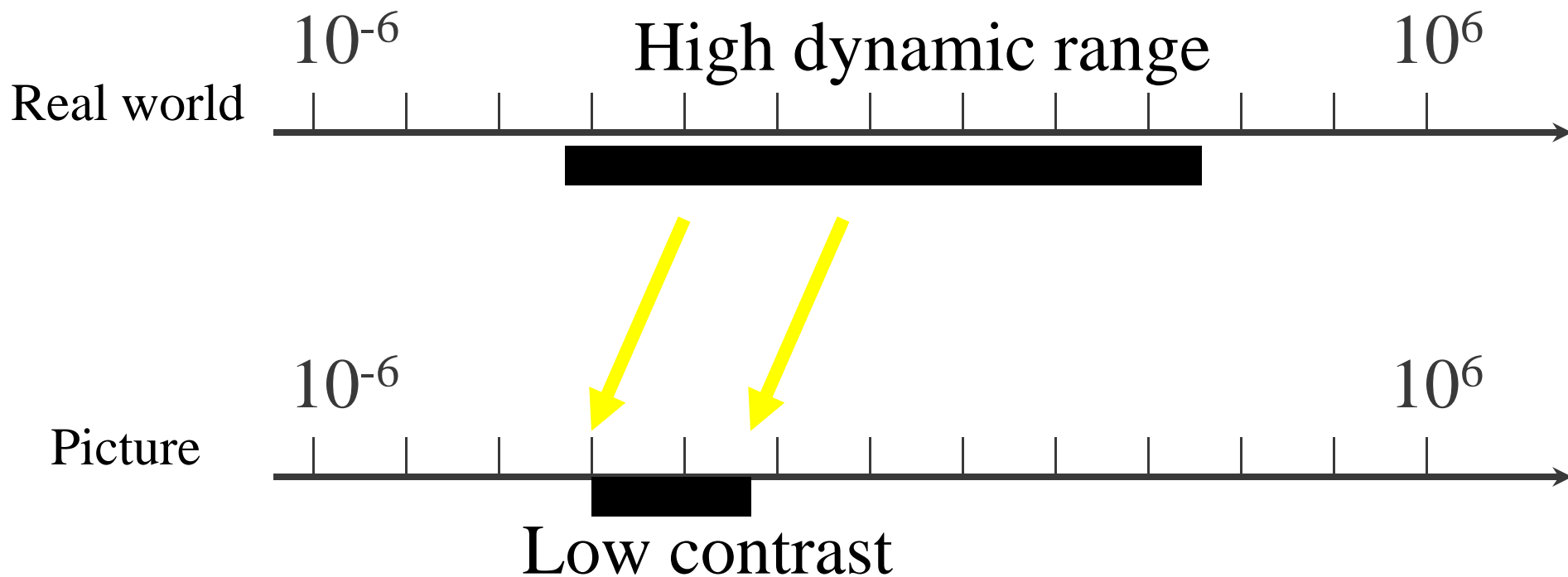
Multiple exposure photography

- Sequentially measure all segments of the range



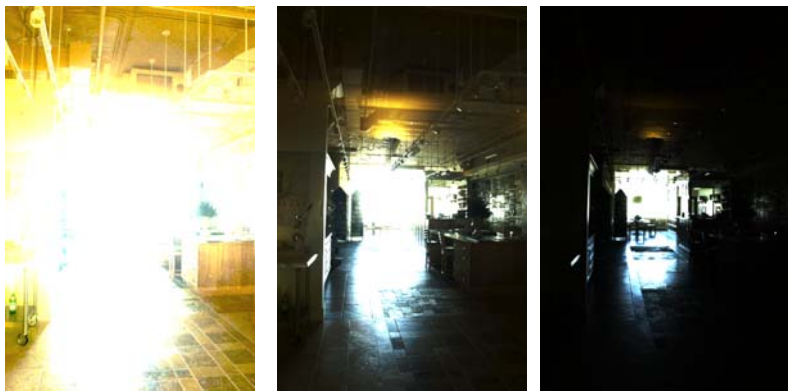
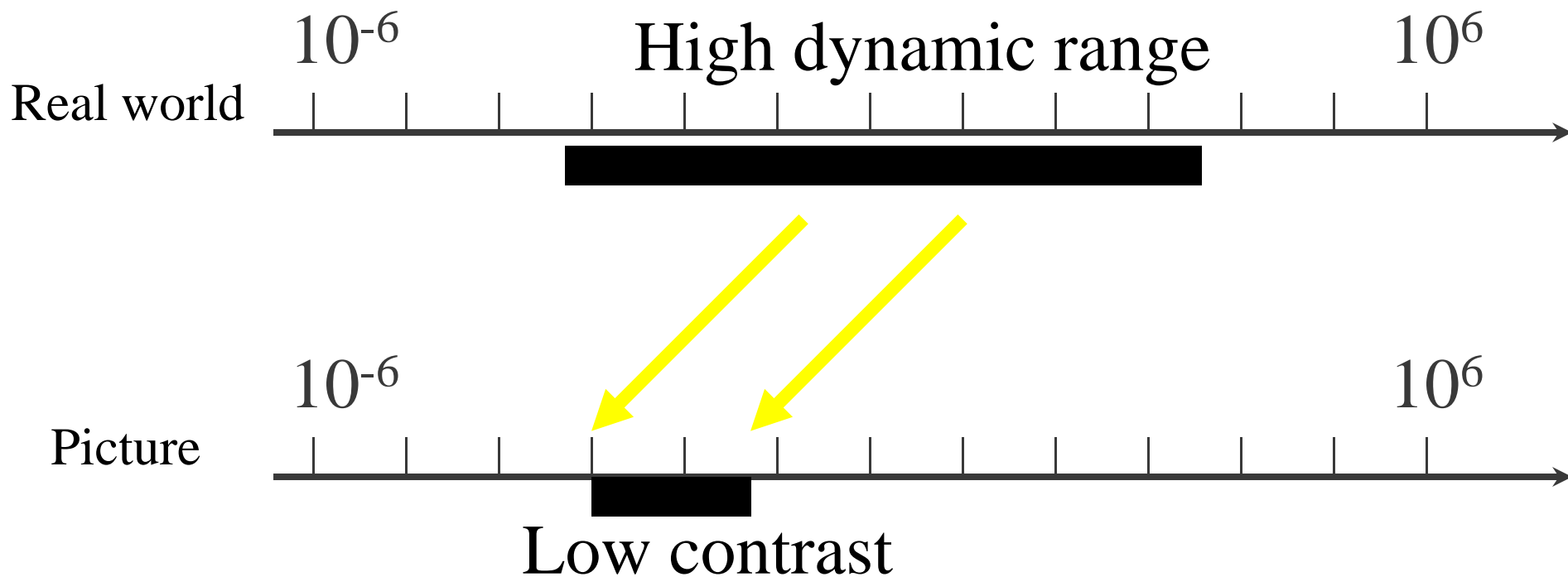
Multiple exposure photography

- Sequentially measure all segments of the range



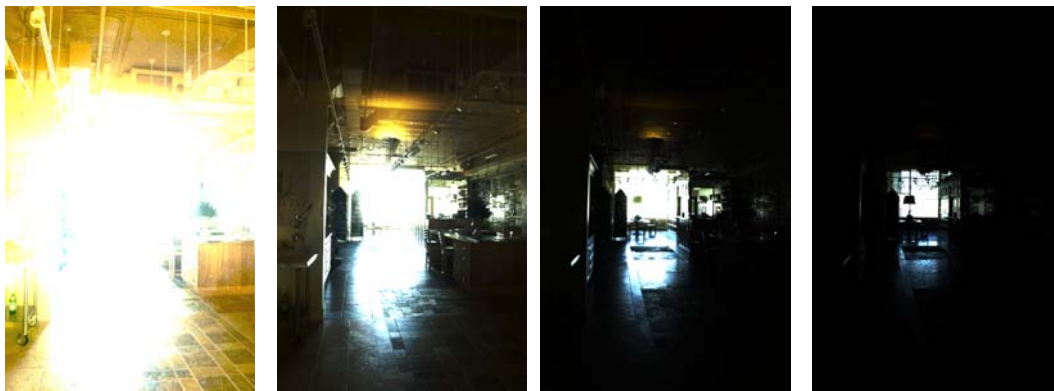
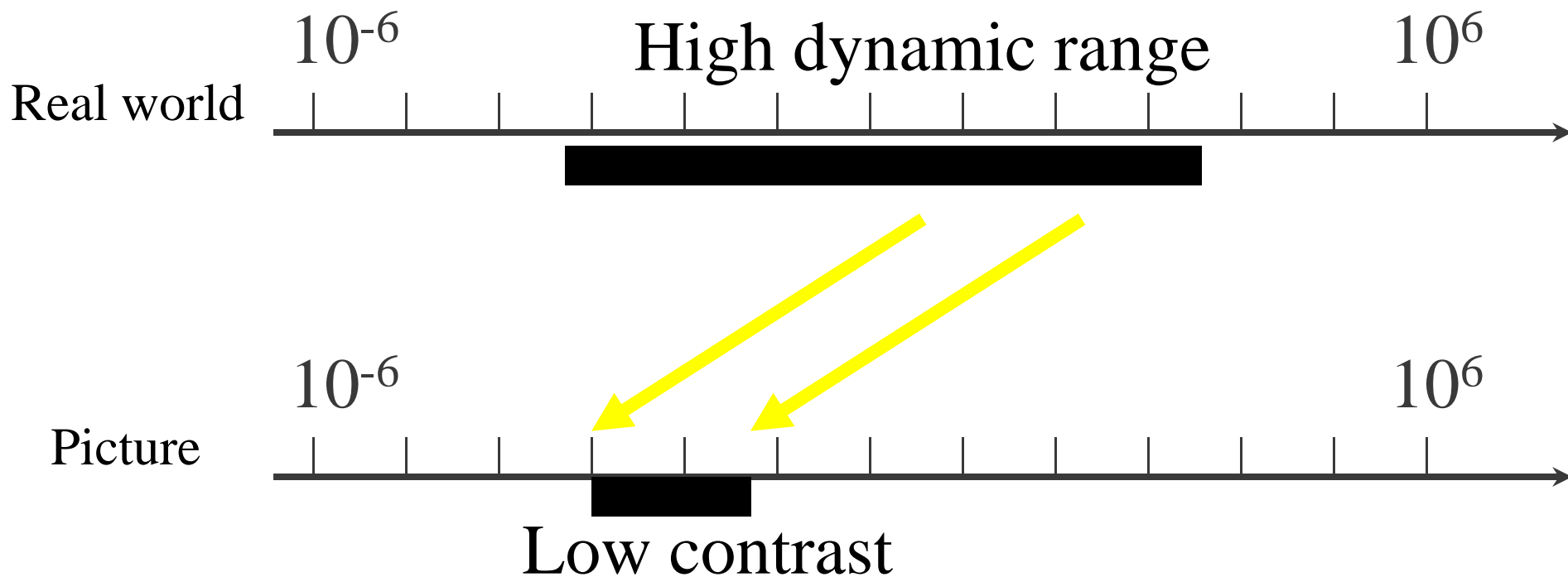
Multiple exposure photography

- Sequentially measure all segments of the range



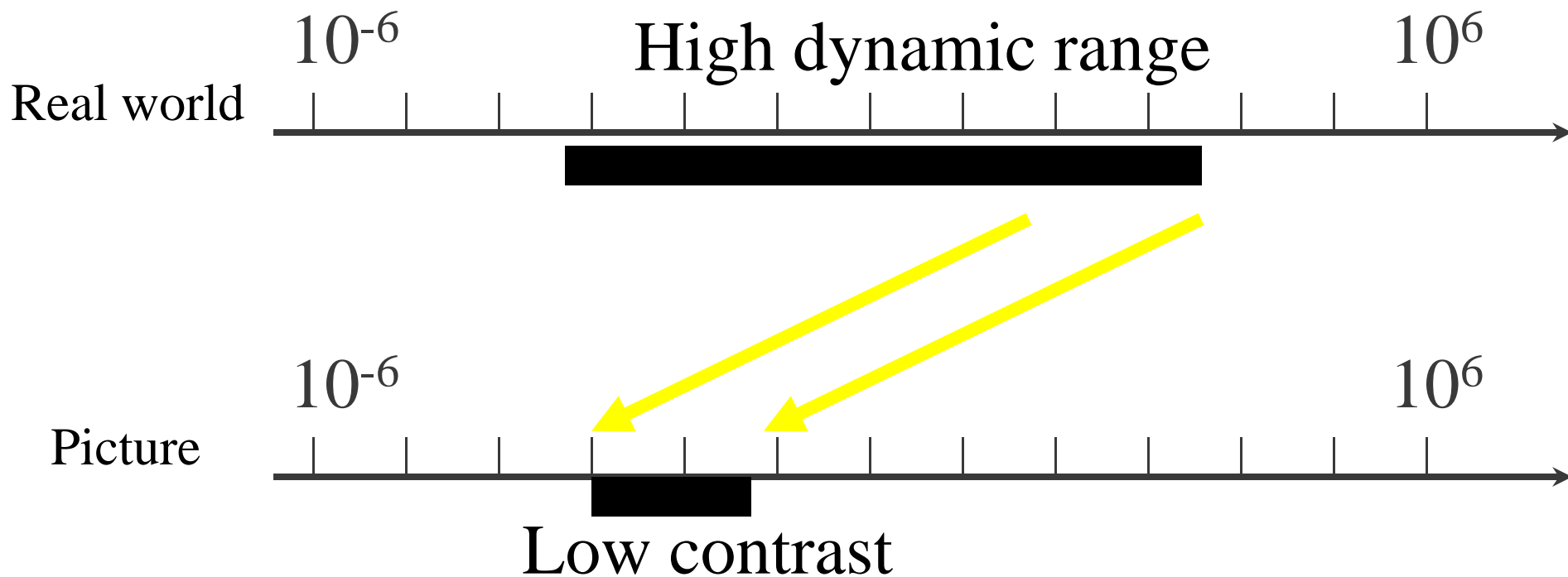
Multiple exposure photography

- Sequentially measure all segments of the range



Multiple exposure photography

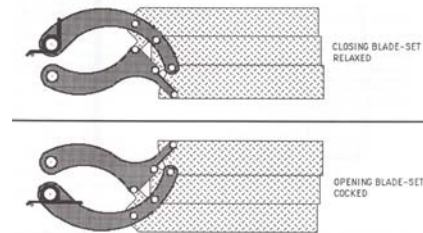
- Sequentially measure all segments of the range



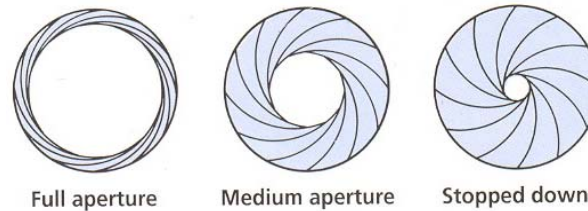
How do we vary exposure?

- **Options:**

- Shutter speed



- Aperture



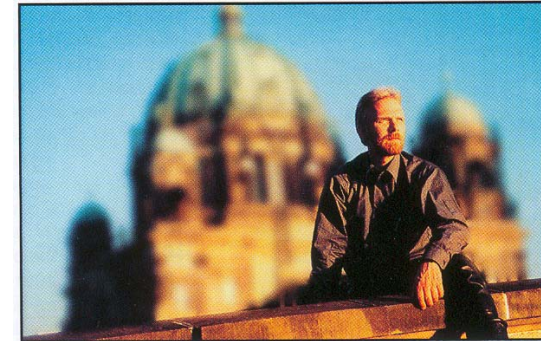
- ISO

- Neutral density filter

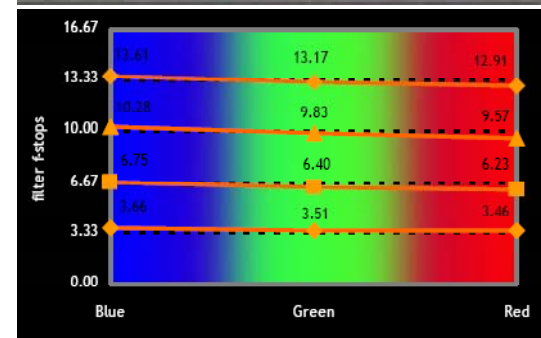


Tradeoffs

- **Shutter speed**
 - Range: ~30 sec to 1/4000sec (6 orders of magnitude)
 - Pros: reliable, linear
 - Cons: sometimes noise for long exposure
- **Aperture**
 - Range: ~f/1.4 to f/22 (2.5 orders of magnitude)
 - Cons: changes depth of field
 - Useful when desperate
- **ISO**
 - Range: ~100 to 1600 (1.5 orders of magnitude)
 - Cons: noise
 - Useful when desperate
- **Neutral density filter**
 - Range: up to 4 densities (4 orders of magnitude) & can be stacked
 - Cons: not perfectly neutral (color shift), not very precise, need to touch camera (shake)
 - Pros: works with strobe/flash, good complement when desperate



Nikon D2X
ISO 3200



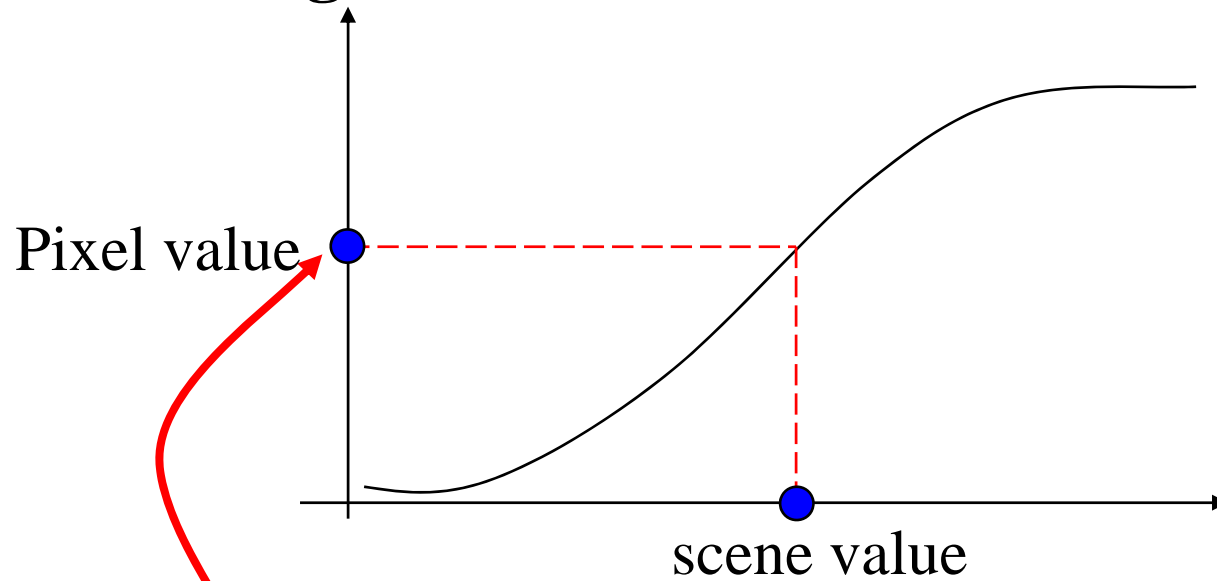
HDR image using multiple exposure

- Given N photos at different exposure
- Recover a HDR color for each pixel



If we know the response curve

- Just look up the inverse of the response curve
- But how do we get the curve?

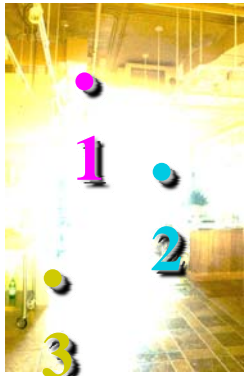


Calibrating the response curve

- **Two basic solutions**
 - Vary scene luminance and see pixel values
 - Assumes we control and know scene luminance
 - Vary exposure and see pixel value for one scene luminance
 - But note that we can usually not vary exposure more finely than by $1/3$ stop
- **Best of both:**
 - Vary exposure
 - Exploit the large number of pixels

The Algorithm

Image series



$\Delta t =$
10 sec



$\Delta t =$
1 sec



$\Delta t =$
1/10 sec



$\Delta t =$
1/100 sec



$\Delta t =$
1/1000 sec

Pixel Value $Z = f(\text{Exposure})$

Exposure = Radiance * Δt

$\log \text{Exposure} = \log \text{Radiance} + \log \Delta t$

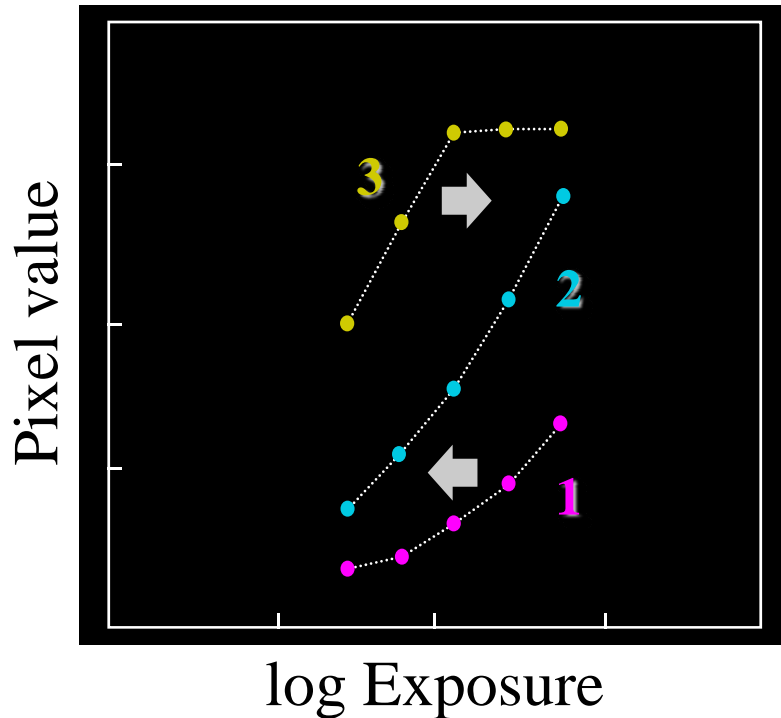
Slide stolen from Fredo Durand who adapted it from Alyosha Efros who borrowed it from Paul Debevec

Δt don't really correspond to pictures. Oh well.

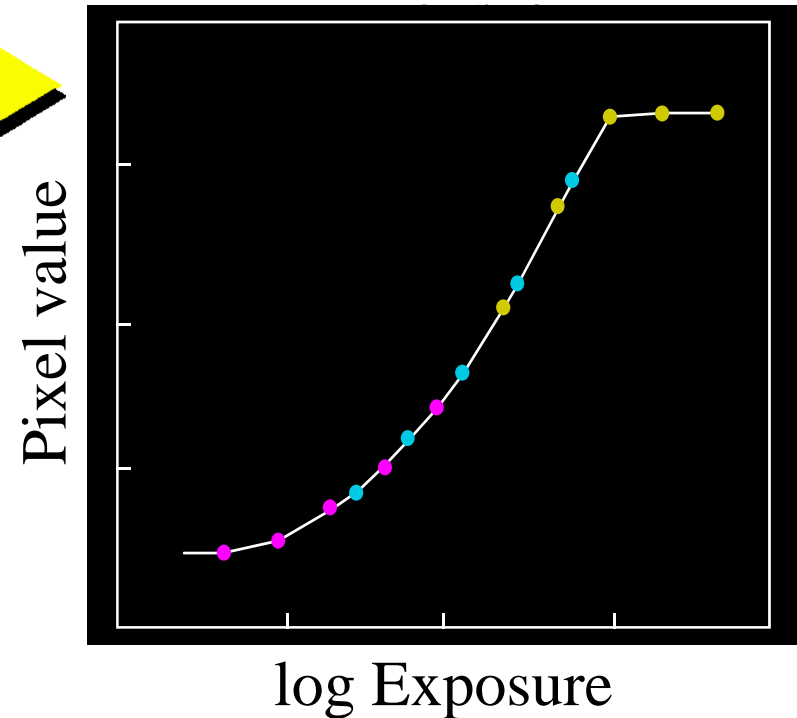
Response curve

- **Exposure is unknown, fit to find a smooth curve**

Assuming unit radiance
for each pixel



After adjusting radiances to
obtain a smooth response



The Math

- Let $g(z)$ be the *discrete* inverse response function
- For each pixel site i in each image j , want:

$$\log \text{Radiance}_\eta + \log \Delta t_j = g(Z_{ij})$$

- Solve the overdetermined linear system:

$$\sum_{i=1}^N \sum_{j=1}^P \left[\log \text{Radiance}_\eta + \log \Delta t_j - g(Z_{ij}) \right]^2 + \lambda \sum_{z=Z_{\min}}^{Z_{\max}} g''(z)^2$$

fitting term smoothness term

Matlab code

```
function [g,lE]=gsolve(Z,B,l,w)

n = 256;
A = zeros(size(Z,1)*size(Z,2)+n+1,n+size(Z,1));
b = zeros(size(A,1),1);

k = 1;           %% Include the data-fitting equations
for i=1:size(Z,1)
    for j=1:size(Z,2)
        wij = w(Z(i,j)+1);
        A(k,Z(i,j)+1) = wij; A(k,n+i) = -wij; b(k,1) = wij * B(i,j);
        k=k+1;
    end
end

A(k,129) = 1;   %% Fix the curve by setting its middle value to 0
k=k+1;

for i=1:n-2     %% Include the smoothness equations
    A(k,i)=1*w(i+1); A(k,i+1)=-2*1*w(i+1); A(k,i+2)=1*w(i+1);
    k=k+1;
end

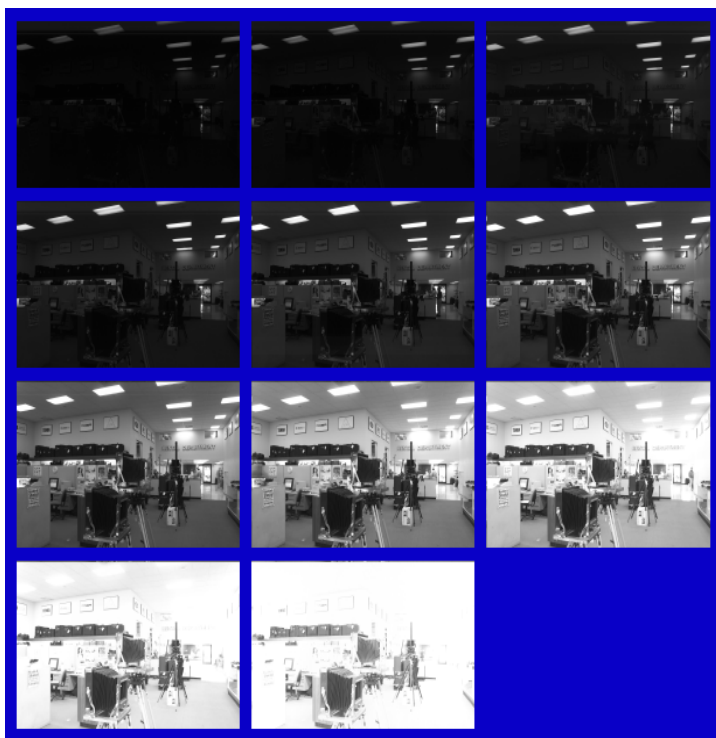
x = A\b;        %% Solve the system using SVD

g = x(1:n);
lE = x(n+1:size(x,1));
```

Result: digital camera

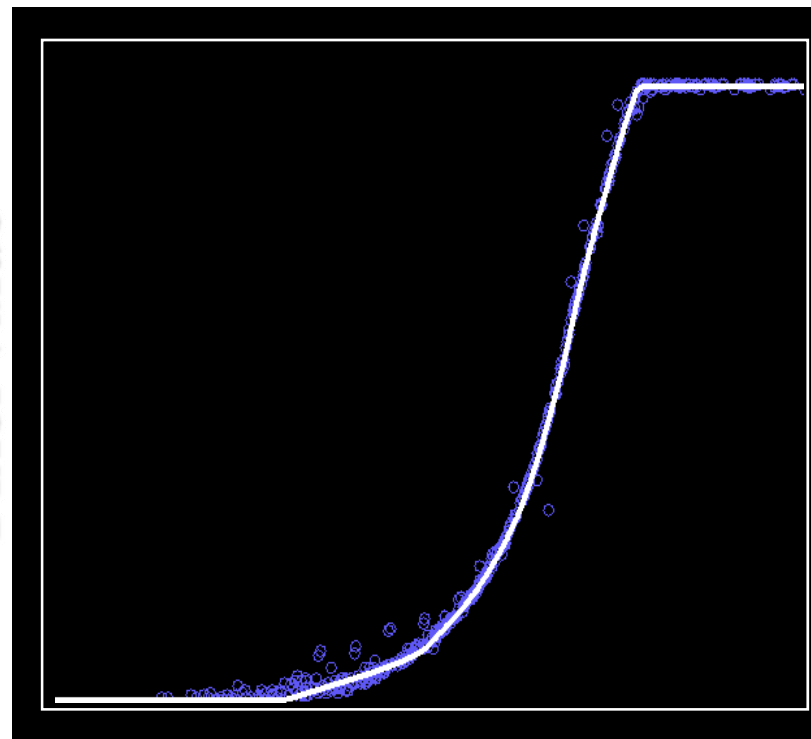
Kodak DCS460

1/30 to 30 sec



Recovered response curve

Pixel value



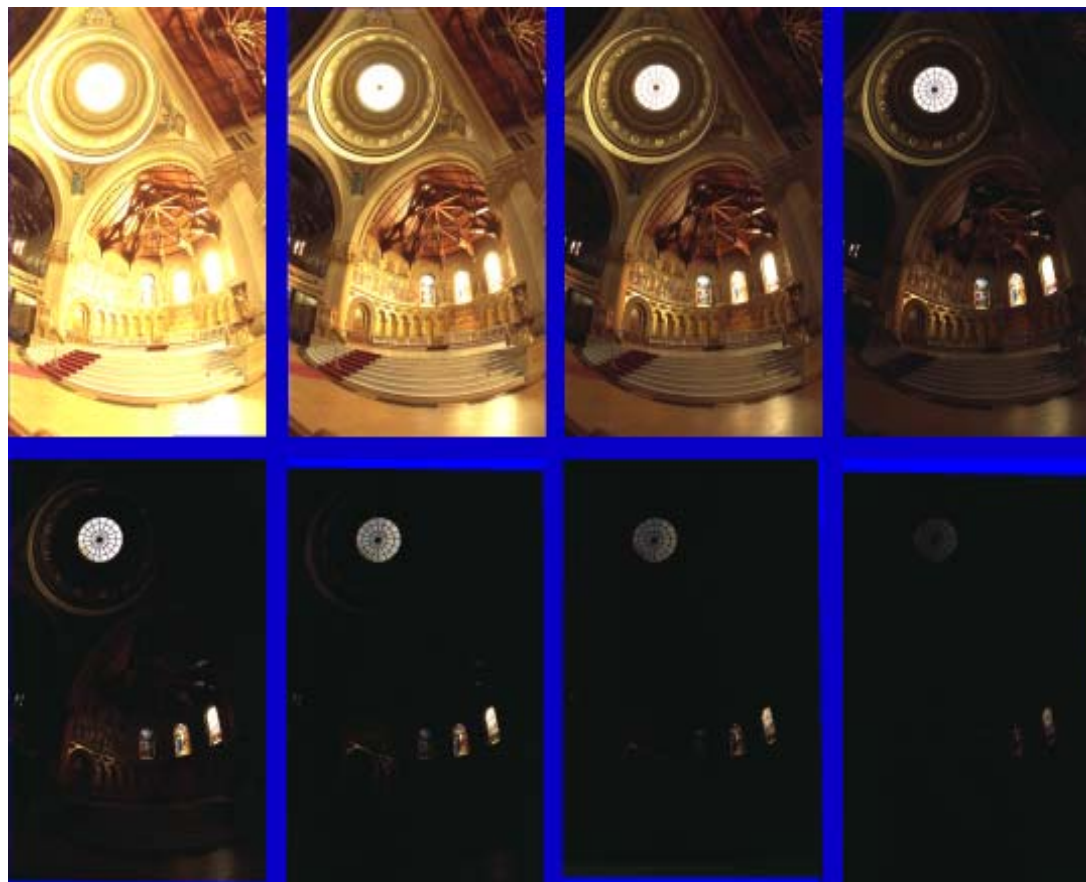
log Exposure

Reconstructed radiance map

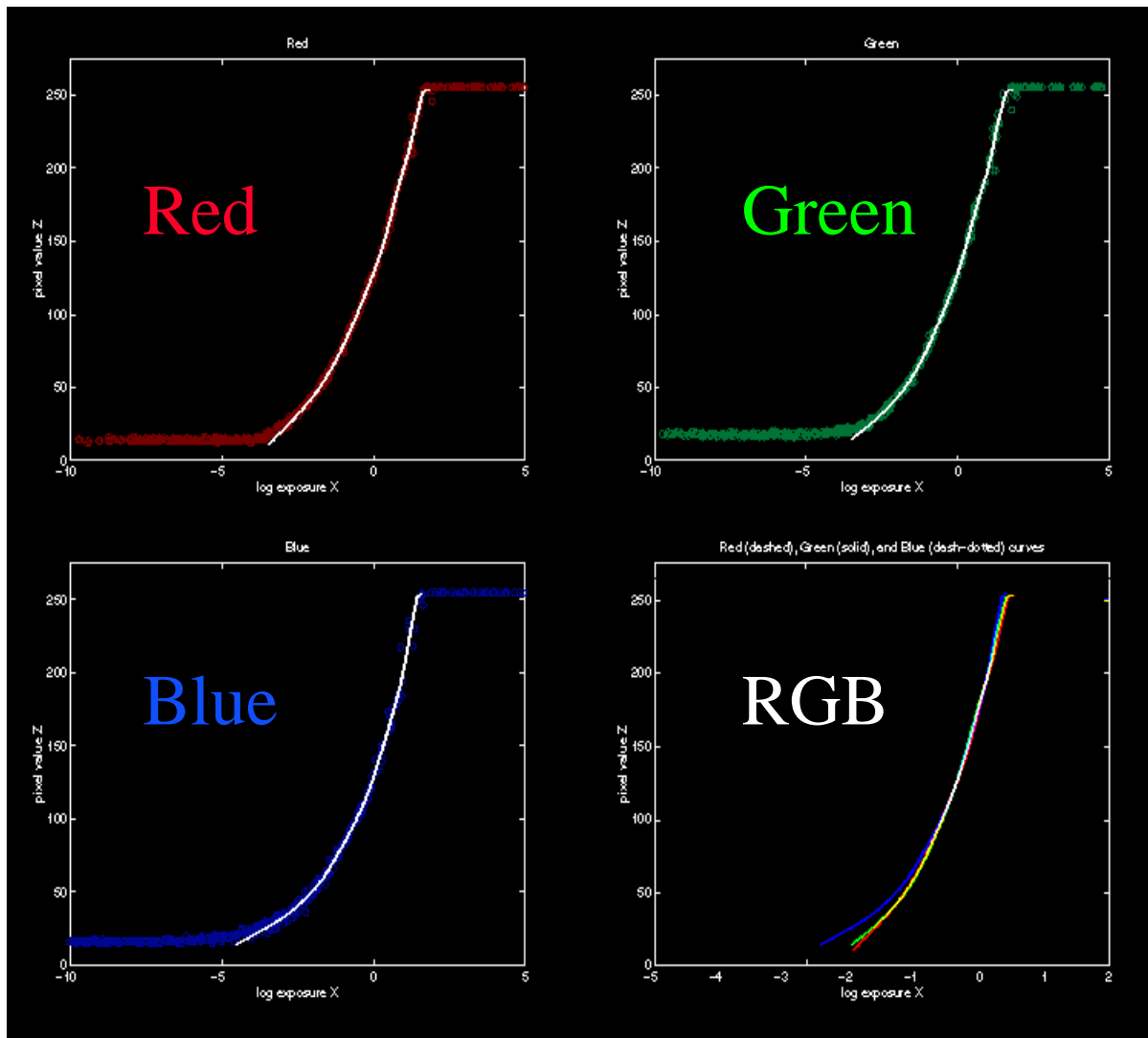


Result: color film

- **Kodak Gold ASA 100, PhotoCD**



Recovered response curves



The Radiance map

W/sr/m²

121.741

28.869

6.846

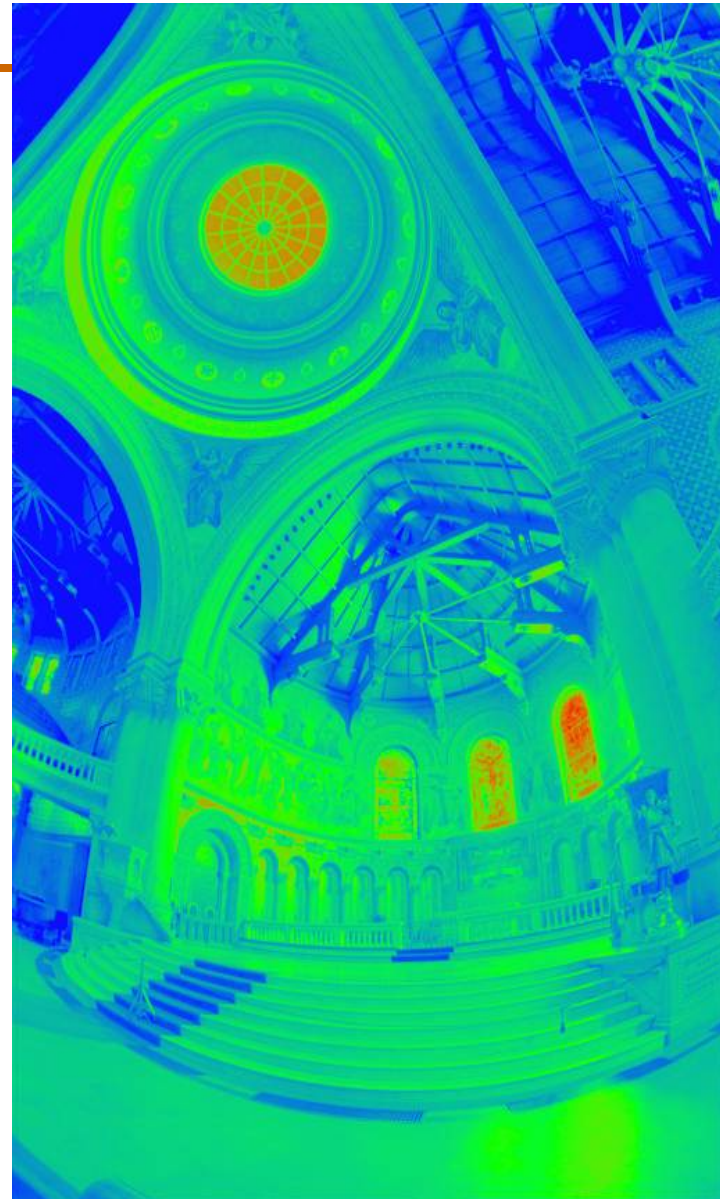
1.623

0.384

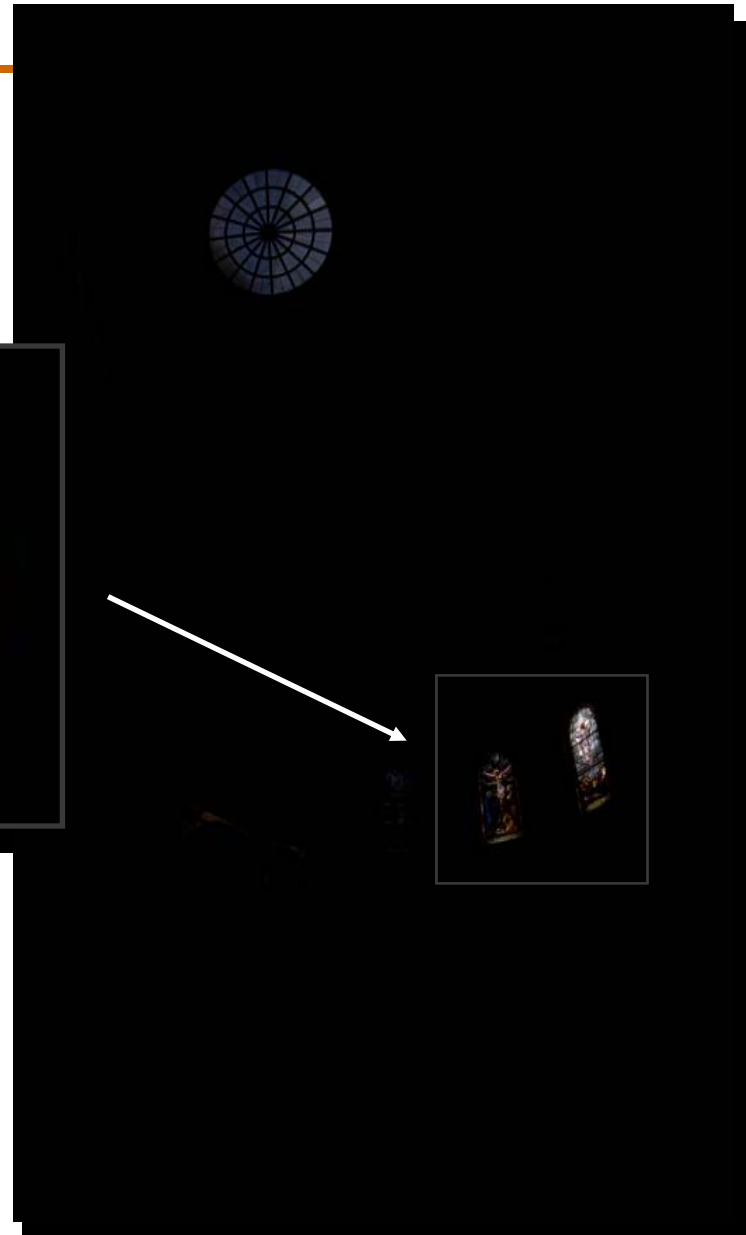
0.091

0.021

0.005



The Radiance map



Linearly scaled to
display device

HDR image processing

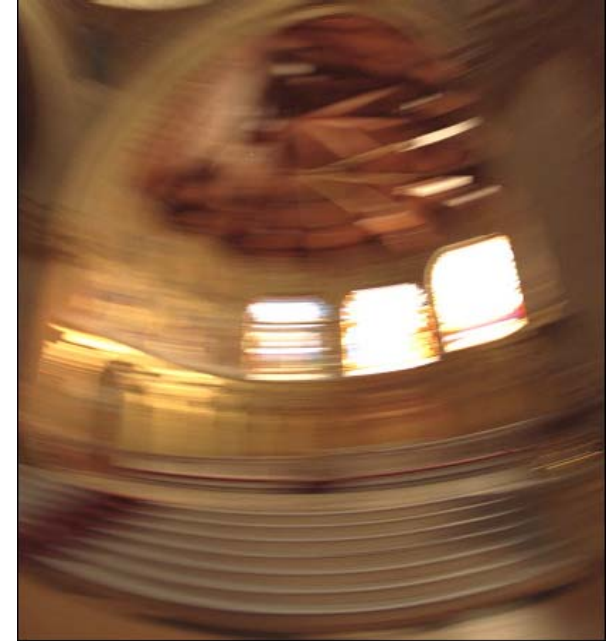
Images from Debevec & Malik 1997



Motion blur applied to **low**-dynamic-range picture



Motion blur applied to **high**-dynamic-range picture



Real motion-blurred picture

- **Important also for depth of field post-process**

Available in HDRShop

H D R S h o p

High Dynamic Range Image Processing and Manipulation



www.debevec.org/HDRShop

[Introduction](#) | [Tutorials](#) | [Reference](#) | [Plugins](#) | [FAQ](#) | [Download/Licensing](#) | [WWW Links](#) | [Mailing List](#)

Chris Tchou et al. *HDR Shop*. S2001 Technical Sketch

Smarter HDR capture

Ward, Journal of Graphics Tools, 2003

<http://www.anywhere.com/gward/papers/jgtpap2.pdf>

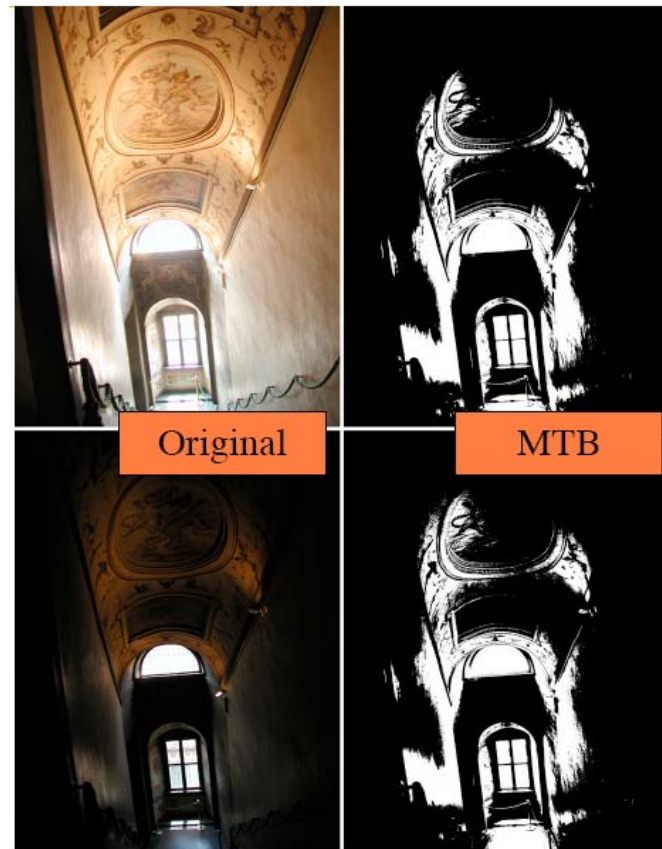
Implemented in Photosphere <http://www.anywhere.com/>

- Image registration (no need for tripod)
- Lens flare removal
- Ghost removal



Image registration

- How to robustly compare images of different exposure?
- Use a black and white version of the image thresholded at the median
 - Median-Threshold Bitmap (MTB)
- Find the translation that minimizes difference
- Accelerate using pyramid



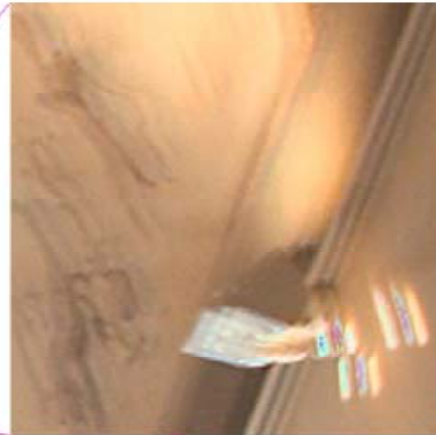


SIGGRAPH2005

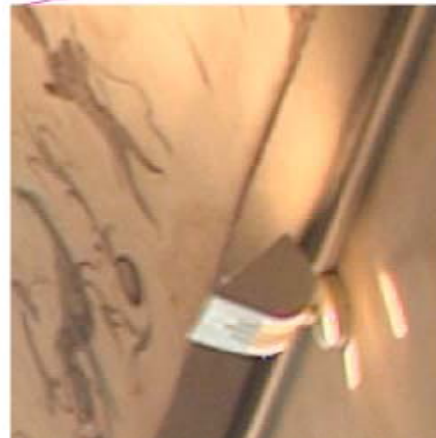
Alignment Results



5 unaligned exposures



Close-up detail



MTB alignment

Time: About .2 second/exposure for 3 MPixel image

Slide from Siggraph 2005 course on HDR

Extension: HDR video

- Kang et al. Siggraph 2003
<http://portal.acm.org/citation.cfm?id=882262.882270>



Figure 1: High dynamic range video of a driving scene. *Top row: Input video with alternating short and long exposures. Bottom row: High dynamic range video (tonemapped).*

Extension: HDR video

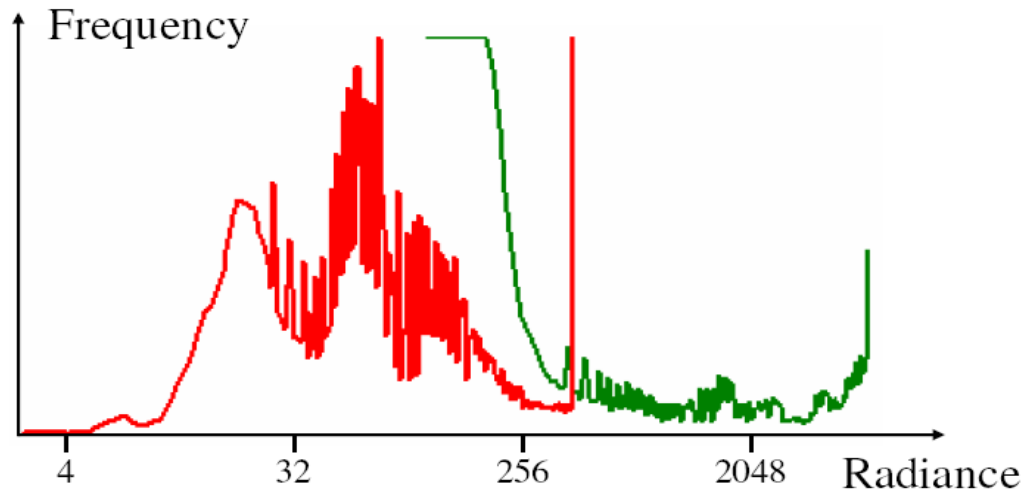


Figure 3: Two input exposures from the driving video. *The radiance histogram is shown on top. The red graph goes with the long exposure frame (bottom left), while the green graph goes with the short exposure frame (bottom right). Notice that the combination of these graphs spans a radiance range greater than a single exposure can capture.*

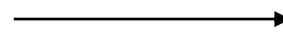
Radiometric camera calibration

(Kim and Pollefeys, PAMI08)

Robustly estimate cameras photometric response curve, exposure and white balance changes of (moving) cameras



video-to-3D



uncalibrated video → photo-consistent HDR video



Radiometric camera calibration

(Kim and Pollefeys, PAMI08)

Robustly estimate cameras photometric response curve, exposure and white balance changes of (moving) cameras



... and also estimate vignetting

original images courtesy of Brown and Lowe



Panorama with vignetting → Compensated panorama



(Kim and Pollefeys, PAMI08)
robust + linear



(Goldman and Chen, ICCV05)
non-linear



(Litvinov and Schechner, CVPR05)
linear



HDR encoding

- **Most formats are lossless**
- **Adobe DNG (digital negative)**
 - Specific for RAW files, avoid proprietary formats
- **RGBE**
 - 24 bits/pixels as usual, plus 8 bit of common exponent
 - Introduced by Greg Ward for Radiance (light simulation)
 - Enormous dynamic range
- **OpenEXR**
 - By Industrial Light + Magic, also standard in graphics hardware
 - 16bit per channel (48 bits per pixel) 10 mantissa, sign, 5 exponent
 - Fine quantization (because 10 bit mantissa), only 9.6 orders of magnitude
- **JPEG 2000**
 - Has a 16 bit mode, lossy

HDR formats

- **Summary of all HDR encoding formats (Greg Ward):**
http://www.anywhere.com/gward/hdrenc/hdr_encodings.html
- **Greg's notes:**
<http://www.anywhere.com/gward/pickup/CIC13course.pdf>
- <http://www.openexr.com/>
- **High Dynamic Range Video Encoding (MPI)** <http://www.mpi-sb.mpg.de/resources/hdrvideo/>

HDR code

- **HDRShop** <http://gl.ict.usc.edu/HDRShop/> (v1 is free)
- **Columbia's camera calibration and HDR combination with source code Mitsunaga, Nayar, Grossberg** http://www1.cs.columbia.edu/CAVE/projects/rad_cal/rad_cal.php
- **Greg Ward Phosphor HDR browser and image combination with registration (Macintosh, command-line version under Linux) with source code** <http://www.anywhere.com/>
- **Photoshop CS2**
- **Idruna** <http://www.idruna.com/photogenicshdr.html>
- **MPI PFS calibration (includes source code)**
<http://www.mpii.mpg.de/resources/hdr/calibration/pfs.html>
- **EXR tools** <http://scanline.ca/exrtools/>
- **HDR Image Editor** <http://www.acm.uiuc.edu/siggraph/HDRIE/>
- **CinePaint** <http://www.cinepaint.org/>
- **Photomatix** <http://www.hdrsoft.com/>
- **EasyHDR** <http://www.astro.leszno.net/easyHDR.php>
- **Artizen HDR** <http://www.supportingcomputers.net/Applications/Artizen/Artizen.htm>
- *Automated High Dynamic Range Imaging Software & Images* http://www2.cs.uh.edu/~somalley/hdri_images.html
- **Optipix** <http://www.imaging-resource.com/SOFT/OPT/OPT.HTM>

HDR images

- <http://www.debevec.org/Research/HDR/>
- <http://www.mpi-sb.mpg.de/resources/hdr/gallery.html>
- <http://people.csail.mit.edu/fredo/PUBLI/Siggraph2002/>
- <http://www.openexr.com/samples.html>
- <http://www.flickr.com/groups/hdr/>
- http://www2.cs.uh.edu/~somalley/hdri_images.html#hdr_others
- <http://www.anywhere.com/gward/hdrenc/pages/originals.html>
- http://www.cis.rit.edu/mcsl/icam/hdr/rit_hdr/
- <http://www.cs.utah.edu/%7Eereinhard/cdrom/hdr.html>
- http://www.sachform.de/download_EN.html
- <http://lcavwww.epfl.ch/%7Elmeylan/HdrImages/February06/February06.html>
- <http://lcavwww.epfl.ch/%7Elmeylan/HdrImages/April04/april04.html>
- <http://books.elsevier.com/companions/0125852630/hdri/html/images.html>

HDR Cameras

- **HDR sensors using CMOS**

- Use a log response curve
- e.g. SMaL,

- **Assorted pixels**

- Fuji
- Nayar et al.

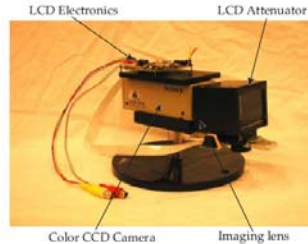


Fuji SuperCCD



- **Per-pixel exposure**

- Filter
- Integration time



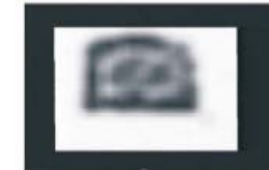
Conventional Camera (without ADR)



Camera with Adaptive Dynamic Range (ADR)



Transmittance Function (LCD Input)



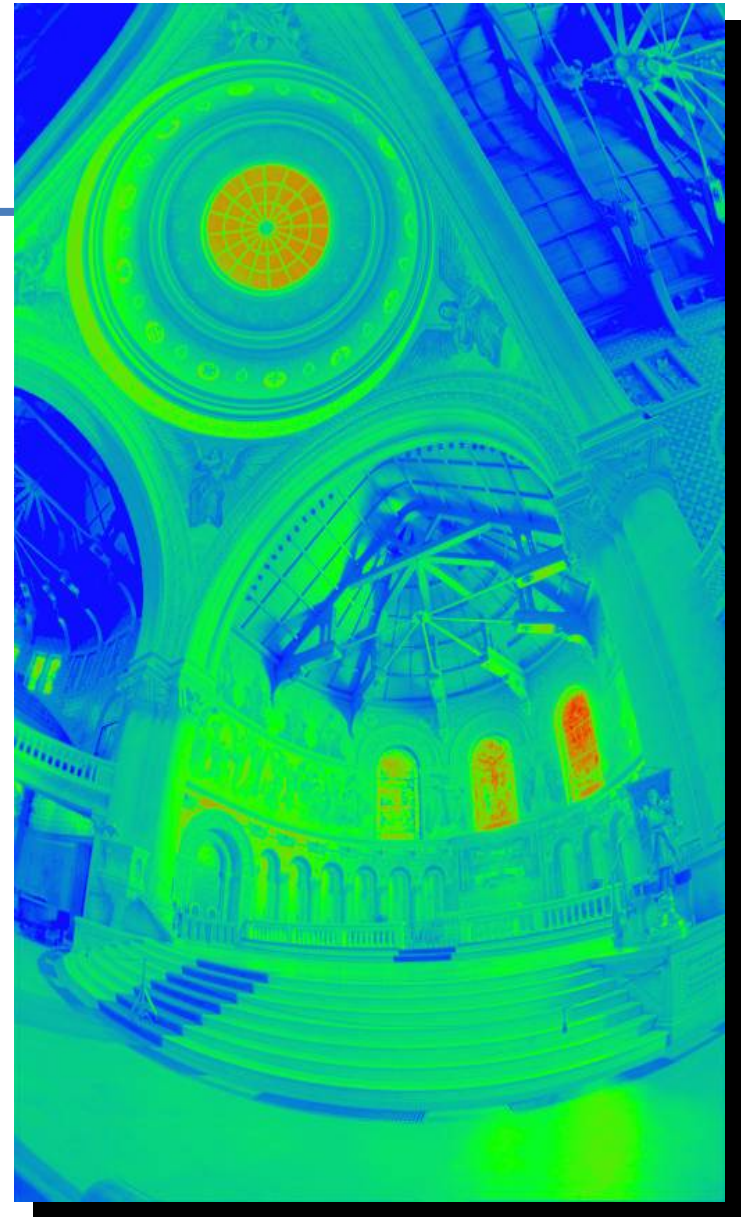
- **Multiple cameras using beam splitters**

- **Other computational photography tricks**

HDR cameras

- <http://www.hdrc.com/home.htm>
- <http://www.smalcamera.com/technology.html>
- <http://www.cfar.umd.edu/~aagrawal/gradcam/gradcam.html>
- <http://www.spheron.com/spheron/public/en/home/home.php>
- <http://www.ims-chips.com/home.php3?id=e0841>
- <http://www.thomsongrassvalley.com/products/cameras/viper/>
- <http://www.pixim.com/>
- <http://www.ptgrey.com/>
- <http://www.siliconimaging.com/>
- <http://www-mtl.mit.edu/researchgroups/sodini/PABLOACO.pdf>
- http://www1.cs.columbia.edu/CAVE/projects/adr_lcd/adr_lcd.php
- http://www1.cs.columbia.edu/CAVE/projects/gen_mos/gen_mos.php
- http://www1.cs.columbia.edu/CAVE/projects/pi_micro/pi_micro.php
- <http://www.cs.cmu.edu/afs/cs/usr/brajovic/www/labweb/index.html>

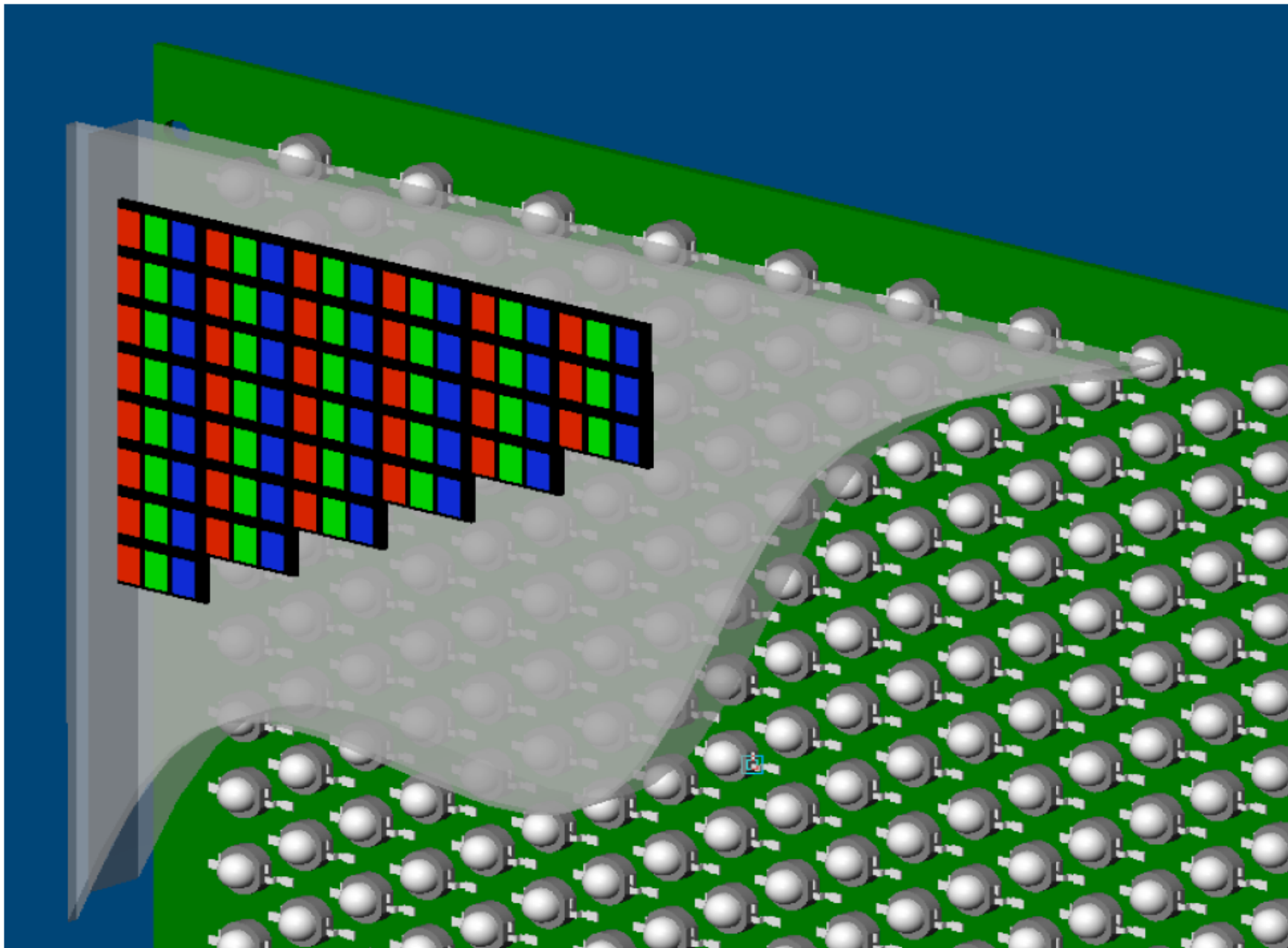
Now What?



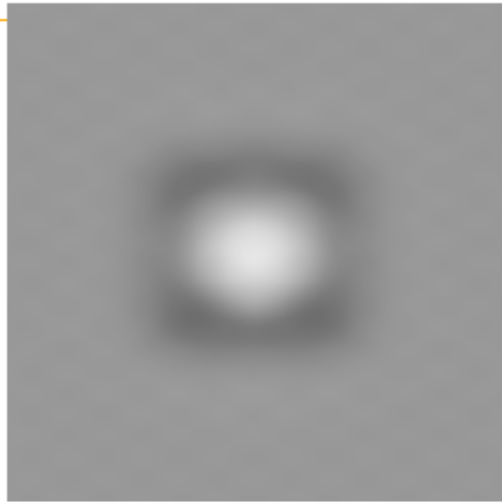
Sunnybrook HDR display

- Use Bright Source + Two 8-bit Modulators
 - Transmission multiplies together
 - Over 10,000:1 dynamic range possible



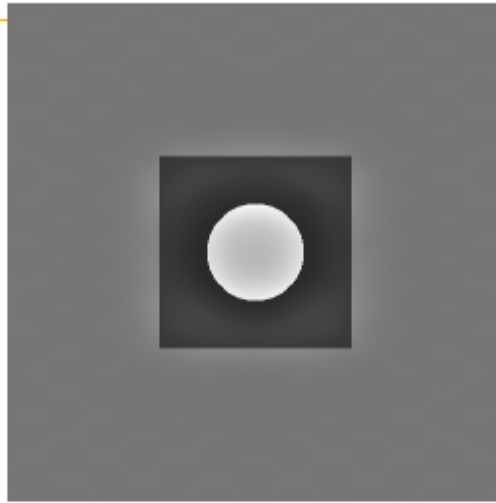


How It Works



LED Backlight

×

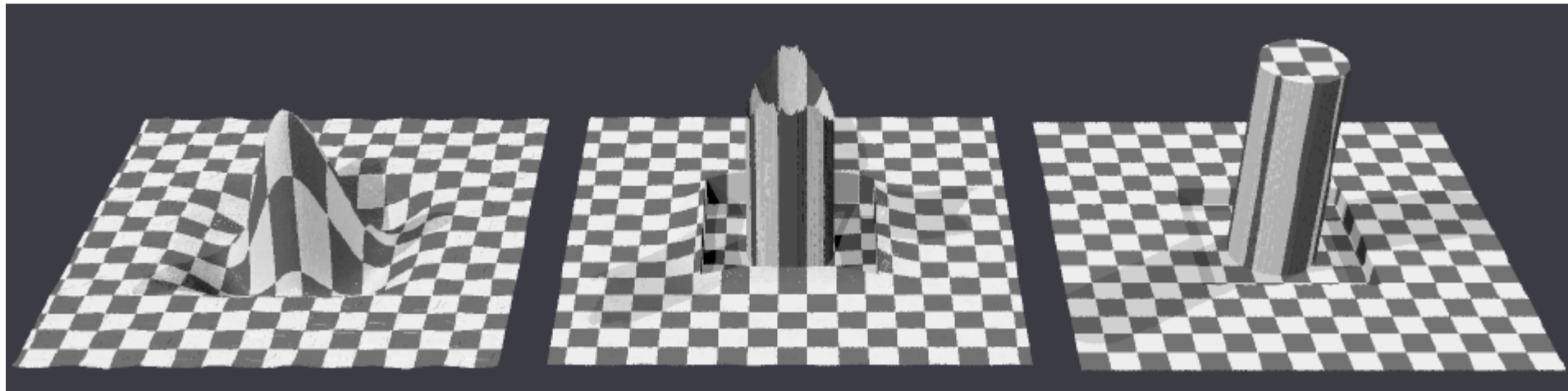


LCD Screen

=



Combined Result

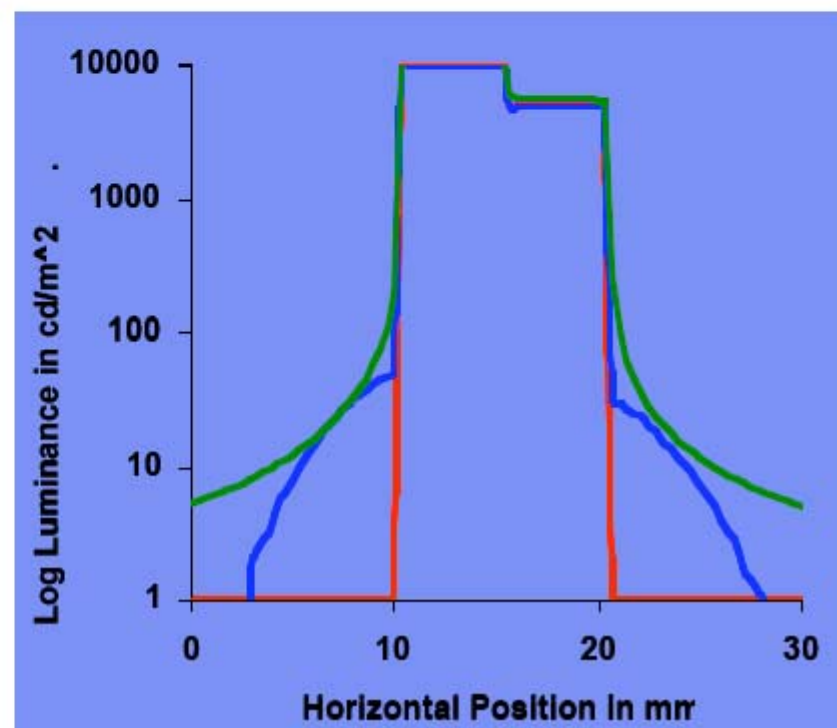
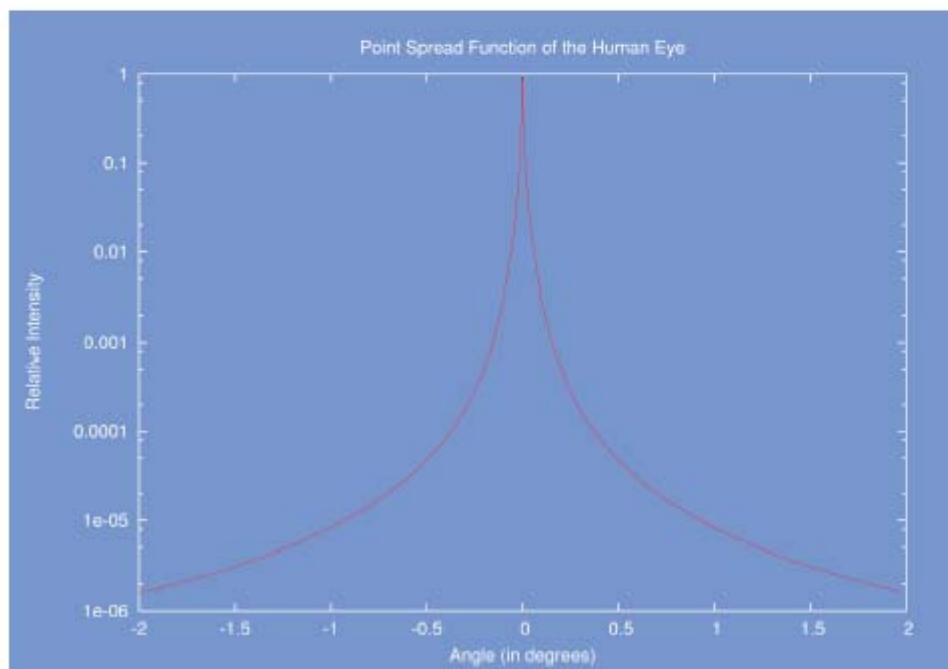


What If Edge Contrast Exceeds LCD Range?



SIGGRAPH2005

Observers cannot tell when this happens because the eye has limited local contrast capacity due to scattering



See Seetzen et al.. SIGGRAPH 2004





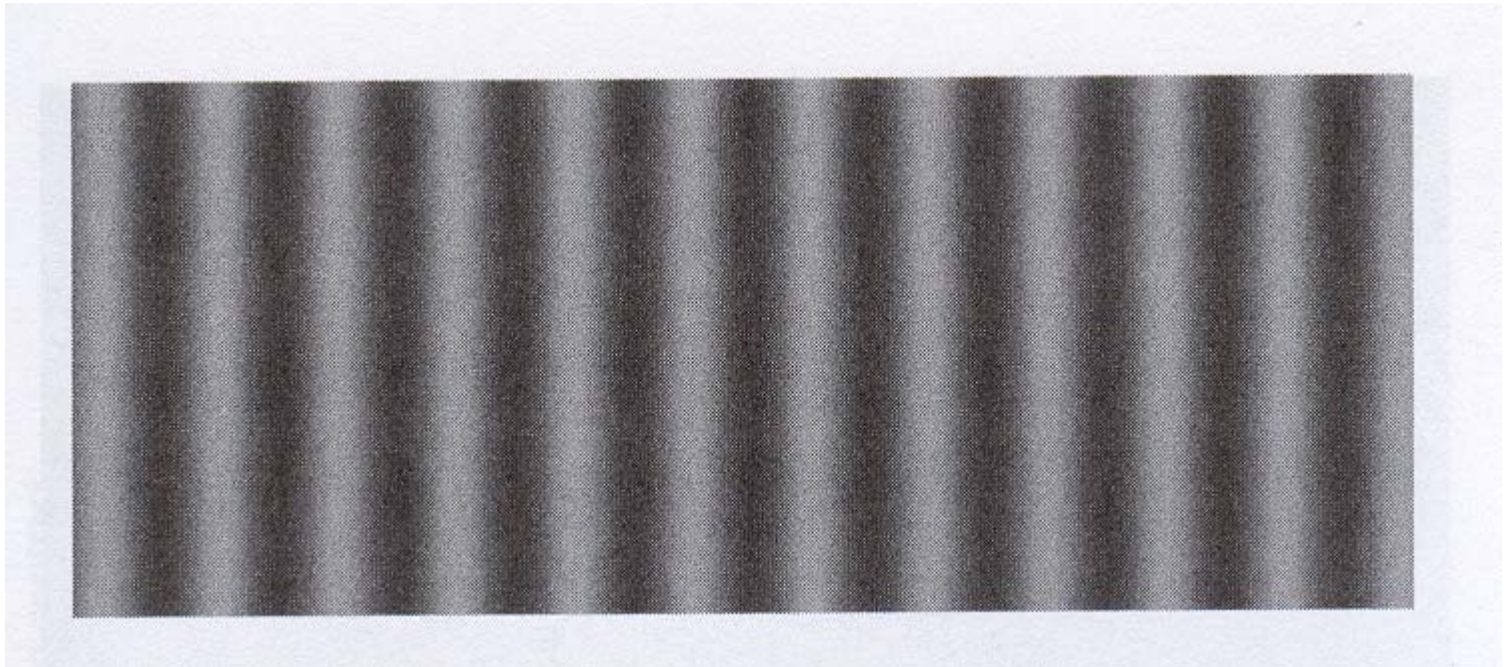
BrightSide DR37-P (now Dolby)

How humans deal with dynamic range

- We're sensitive to contrast (multiplicative)
 - A ratio of 1:2 is perceived as the same contrast as a ratio of 100 to 200
 - Makes sense because illumination has a multiplicative effect
 - Use the log domain as much as possible
- Dynamic adaptation (very local in retina)
 - Pupil (not so important)
 - Neural
 - Chemical
- Different sensitivity to spatial frequencies

Contrast Sensitivity

- Sine Wave grating
- What contrast is necessary to make the grating visible?



Contrast Sensitivity Function (CSF)

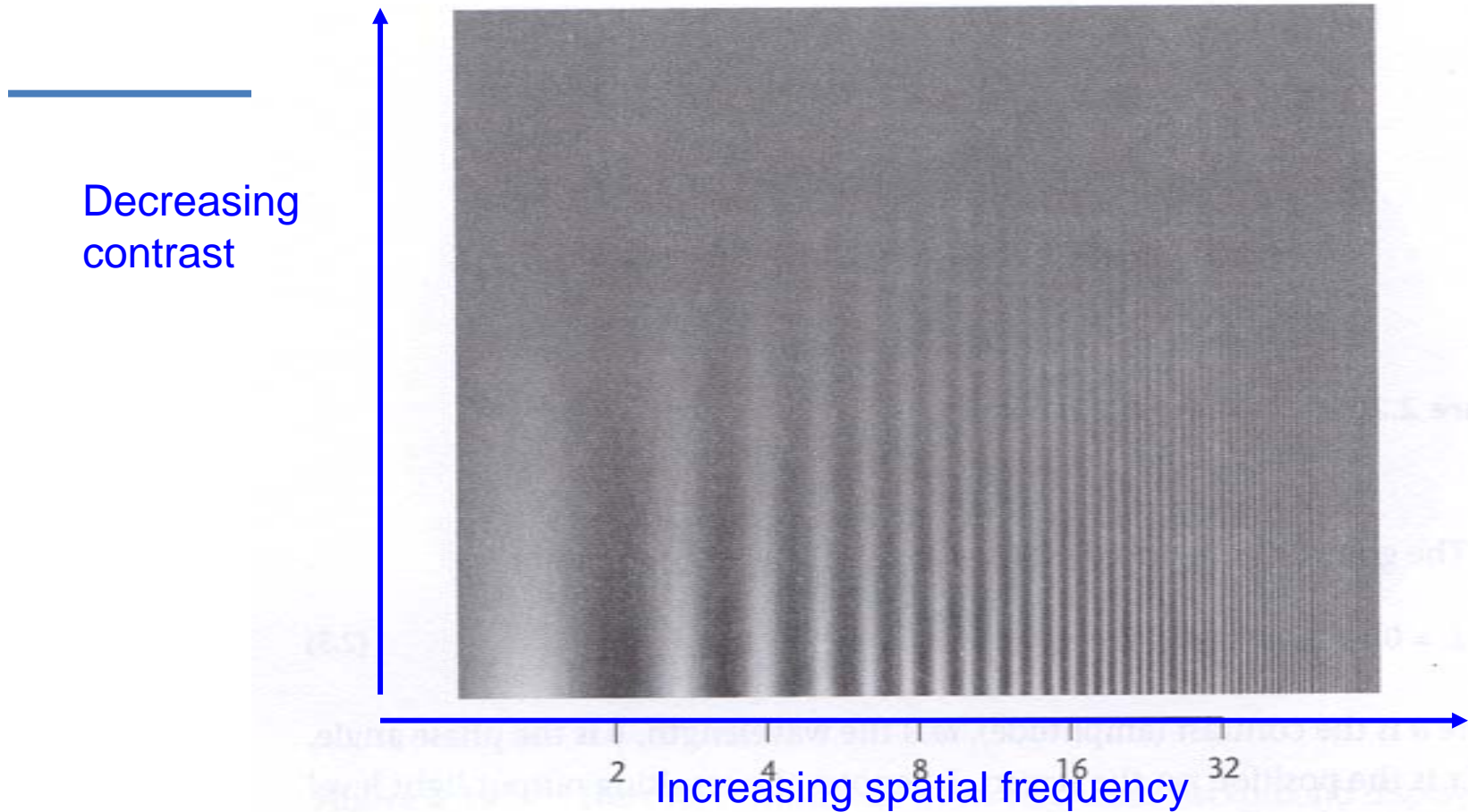


Figure 2.21

This grating pattern changes frequency exponentially from left to right and varies in contrast in a vertical direction. The highest frequency you can resolve depends on the distance from which you view the pattern. The scale gives the spatial frequency if it is viewed from 2.3 m.

Contrast Sensitivity Function (CSF)

- Low sensitivity to low frequencies
- Importance of medium to high frequencies
- Most methods to deal with dynamic range reduce the contrast of low frequencies
- But keep the color

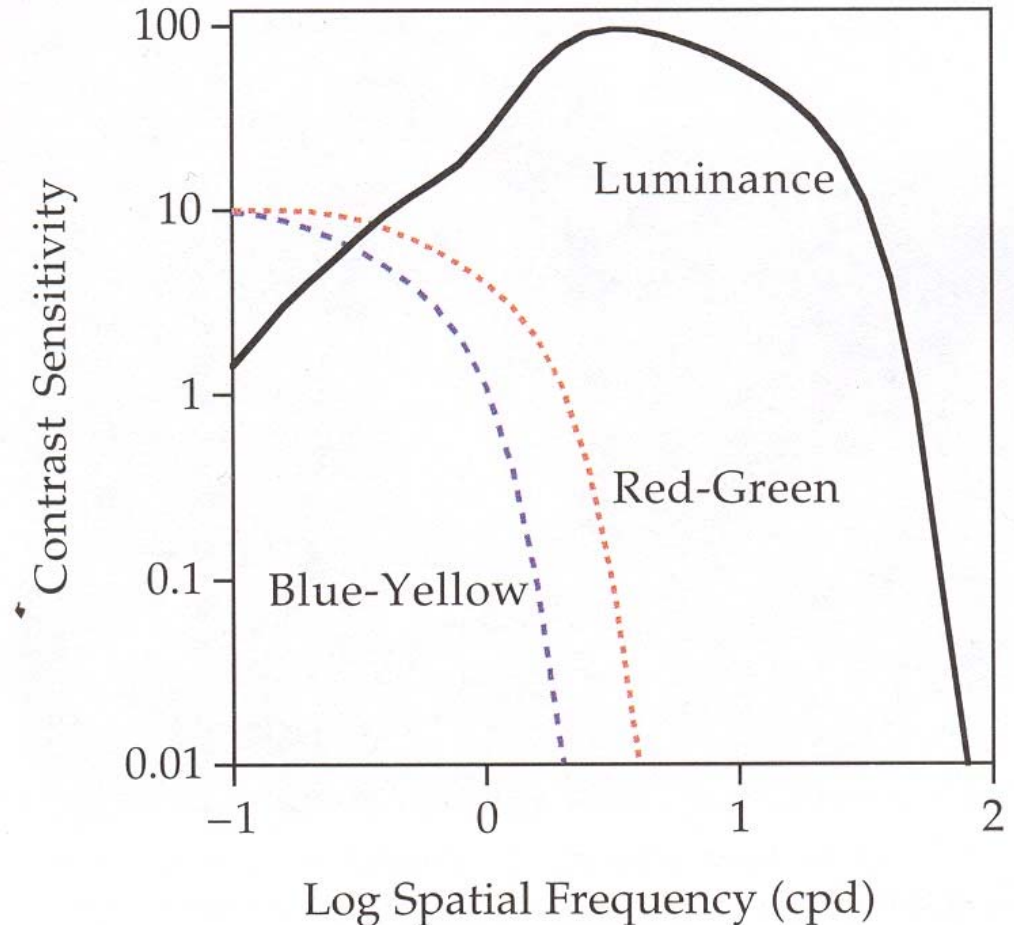


Figure 1-18. Spatial contrast sensitivity functions for luminance and chromatic contrast.

The second half: contrast reduction



- **Input: high-dynamic-range image**
 - (floating point per pixel)



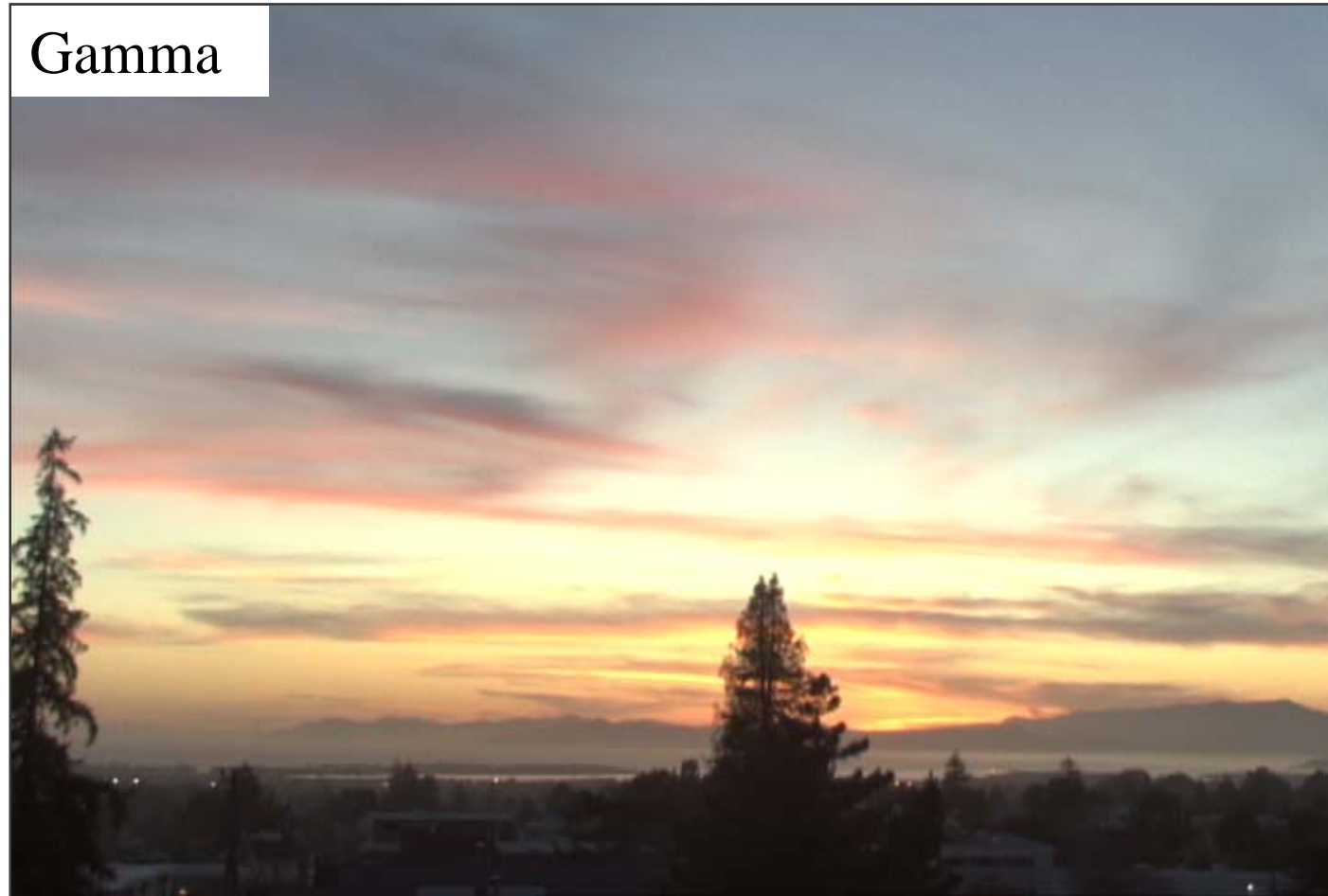
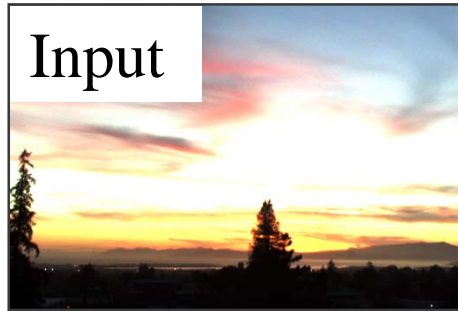
Naïve technique

- Scene has *1:10,000* contrast, display has *1:100*
- Simplest contrast reduction?



Naïve: Gamma compression

- $X \rightarrow X^\gamma$ (where $\gamma=0.5$ in our case)
- But... colors are washed-out. Why?



Gamma compression on intensity

- Colors are OK,
but details (intensity high-frequency) are blurred

Intensity



Gamma on intensity

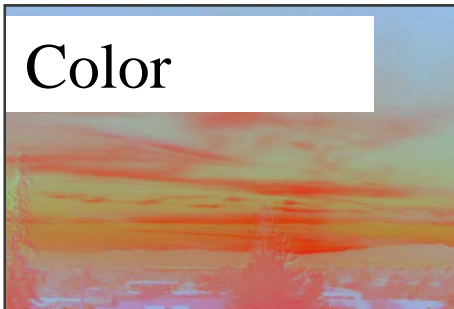


Color



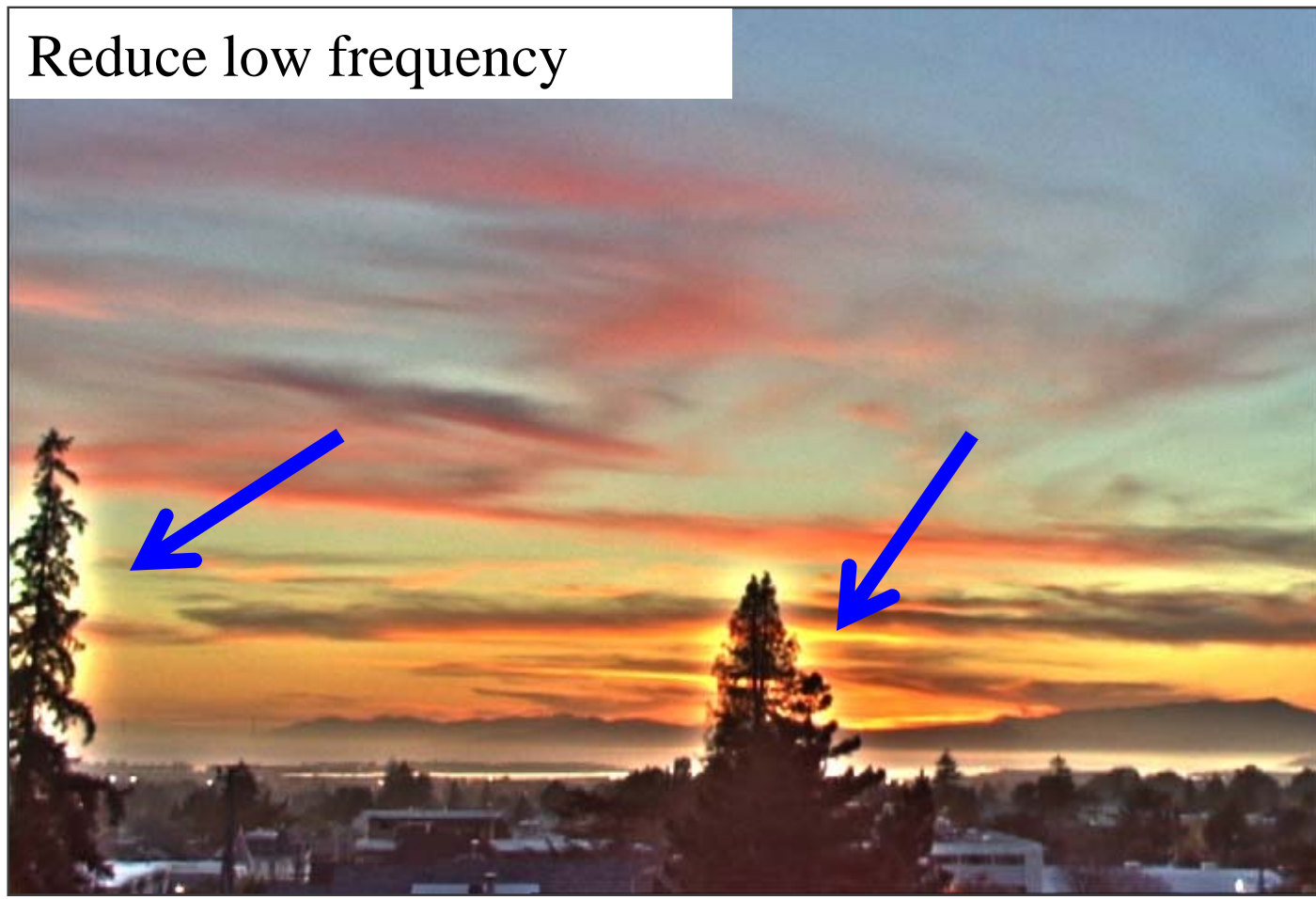
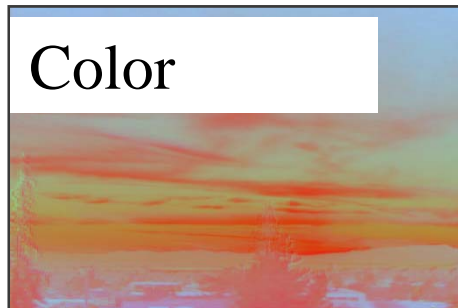
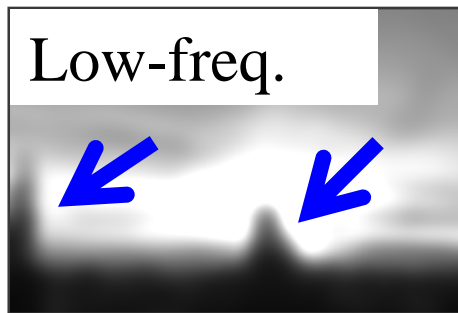
Oppenheim 1968, Chiu et al. 1993

- Reduce contrast of low-frequencies
- Keep high frequencies



The halo nightmare

- For strong edges
- Because they contain high frequency



Our approach

- **Do not blur across edges**
- **Non-linear filtering**

Large-scale



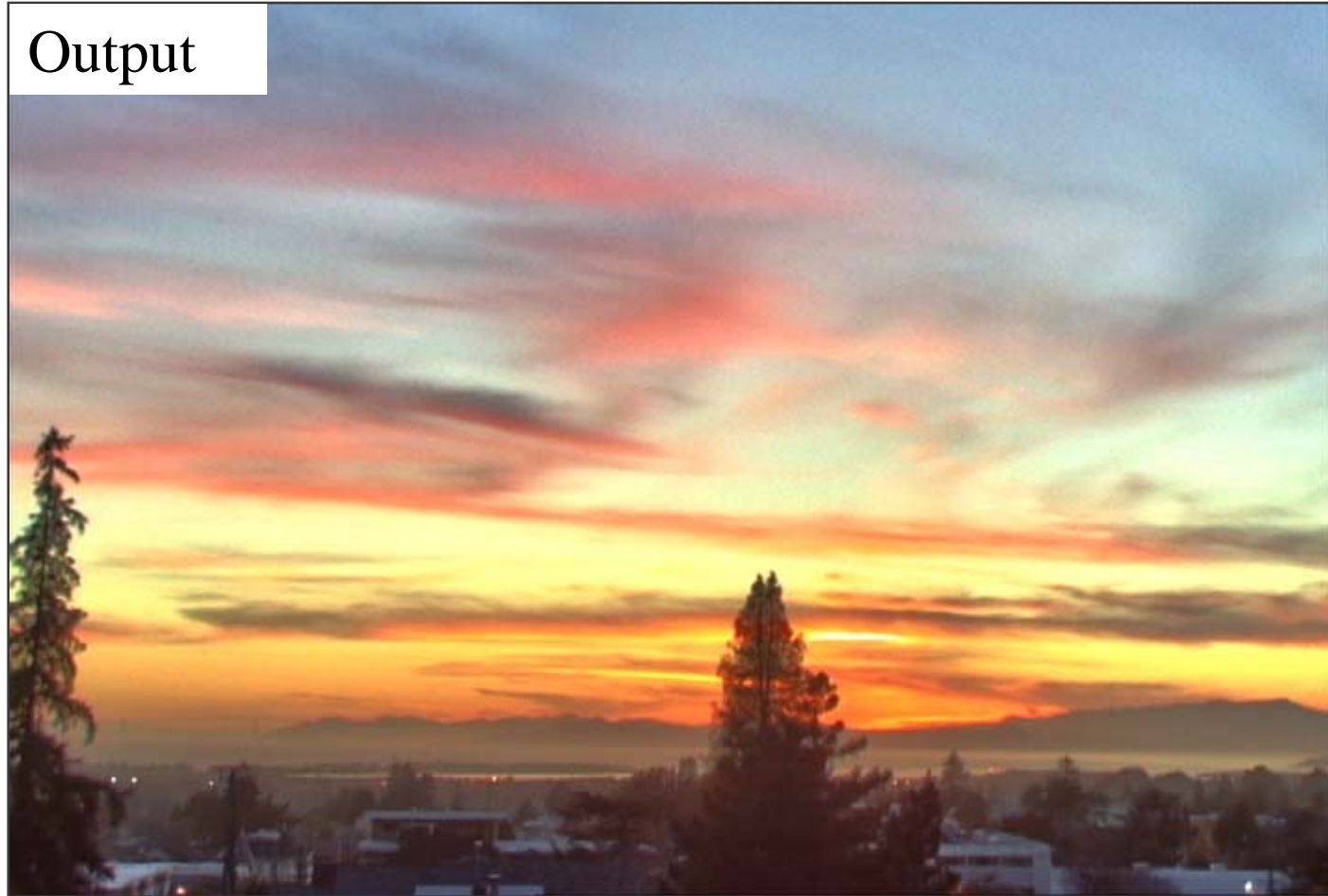
Detail



Color



Output



Bilateral filter

- **Tomasi and Manduci 1998**

<http://www.cse.ucsc.edu/~manduchi/Papers/ICCV98.pdf>

- **Related to**

- SUSAN filter

[Smith and Brady 95]

<http://citeseer.ist.psu.edu/smith95susan.html>

- Digital-TV [Chan, Osher and Chen 2001]

<http://citeseer.ist.psu.edu/chan01digital.html>

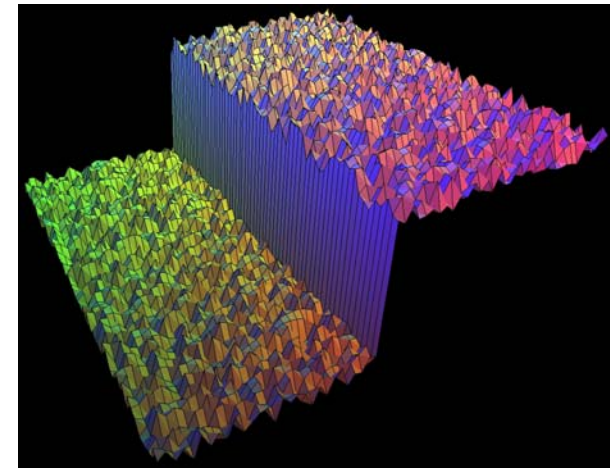
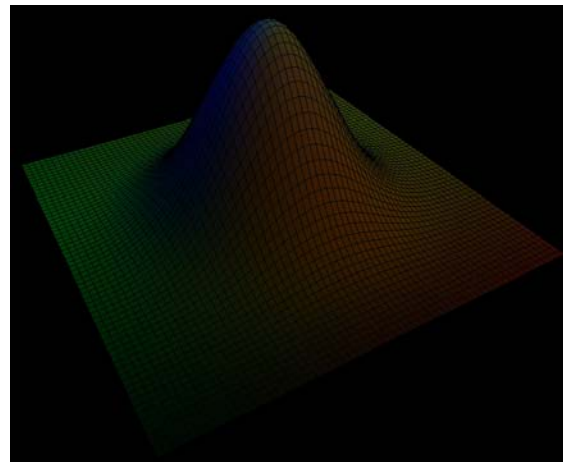
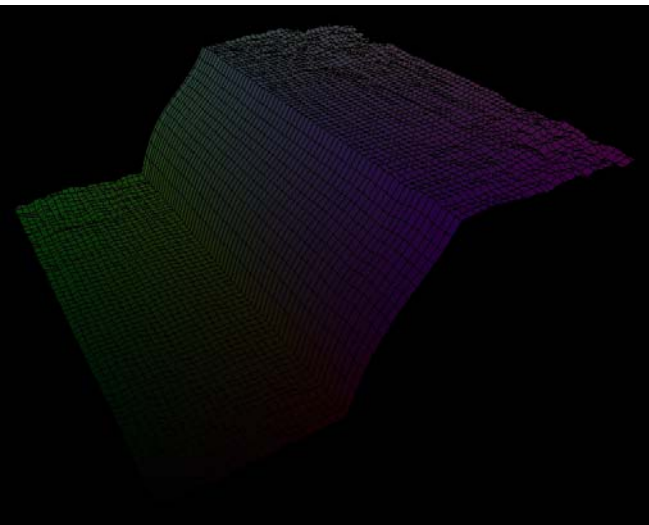
- sigma filter

<http://www.geogr.ku.dk/CHIPS/Manual/f187.htm>

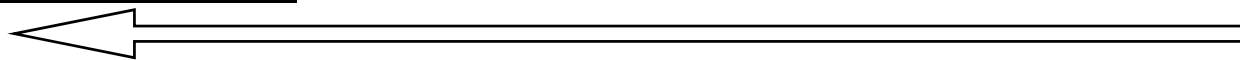
Start with Gaussian filtering

- Here, input is a step function + noise

$$J = f \otimes I$$



output

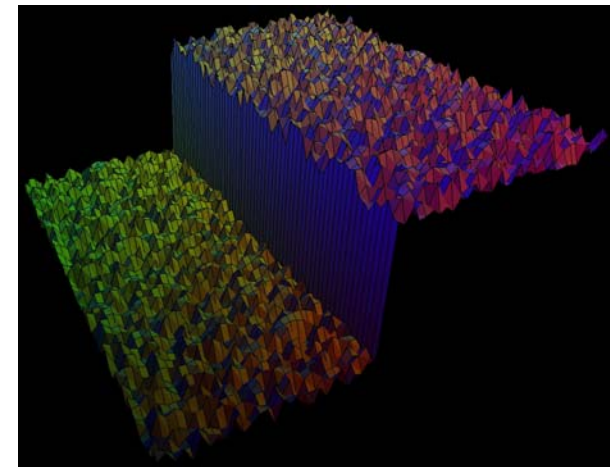
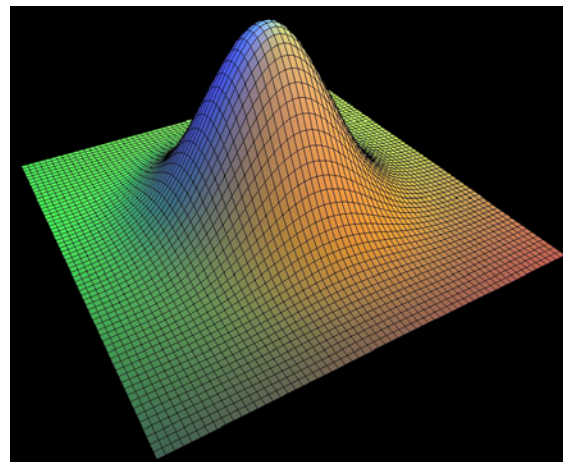
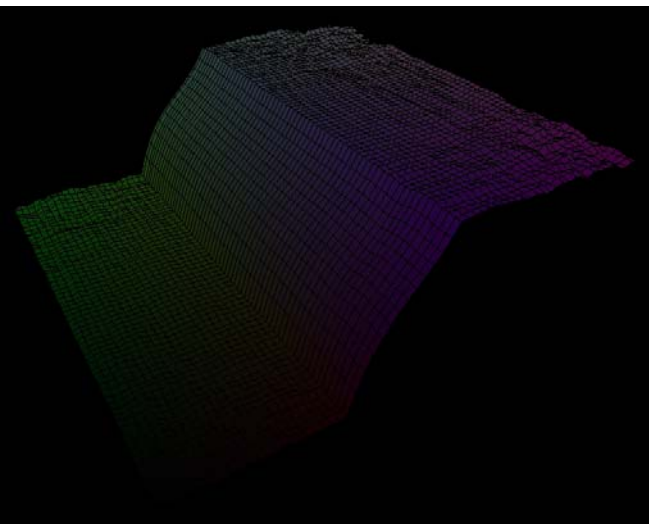


input

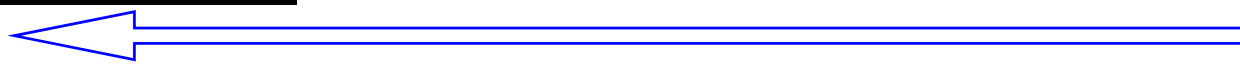
Start with Gaussian filtering

- Spatial Gaussian f

$$J = f \otimes I$$



output

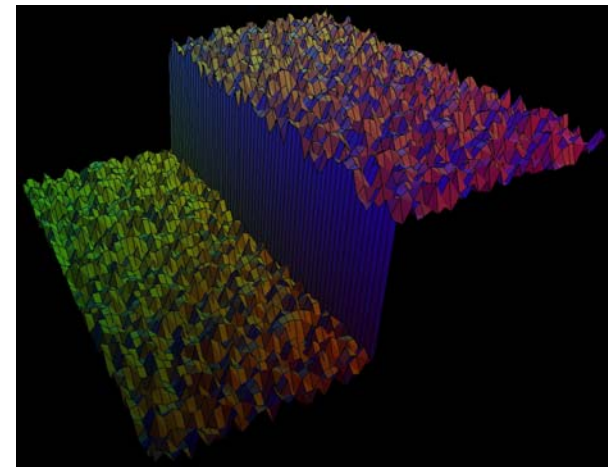
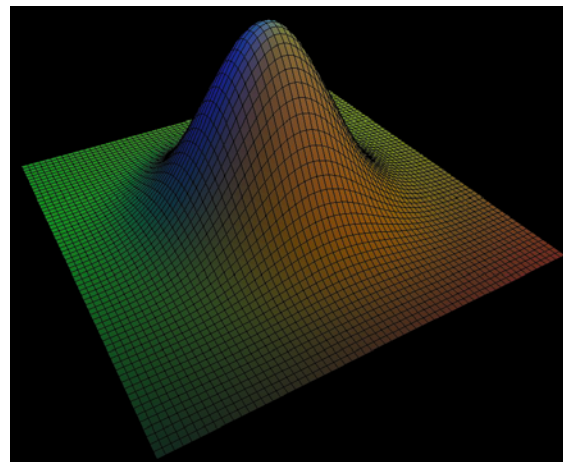
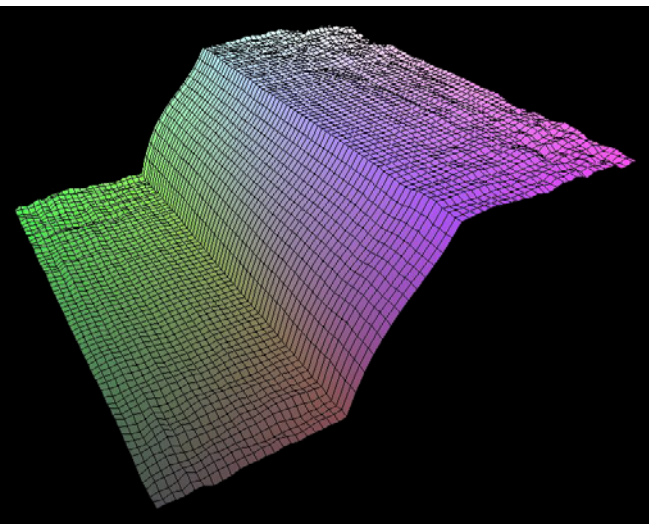


input

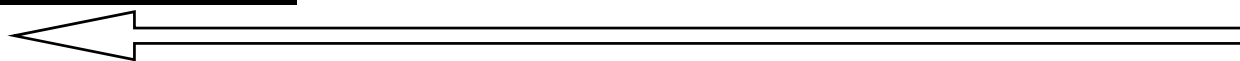
Start with Gaussian filtering

- Output is blurred

$$J = f \otimes I$$



output

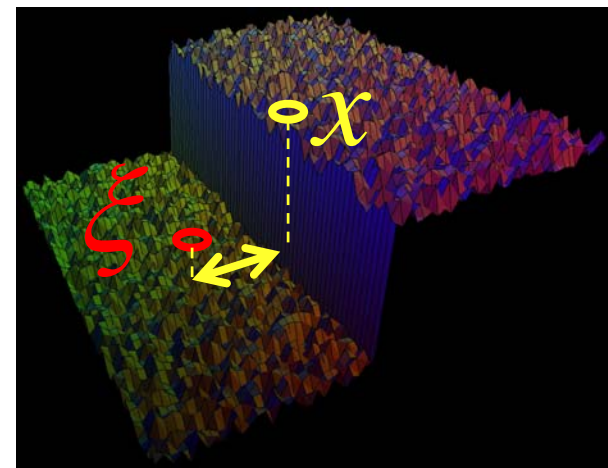
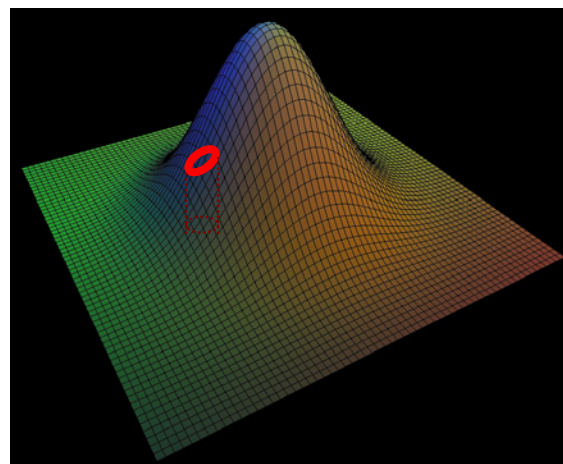
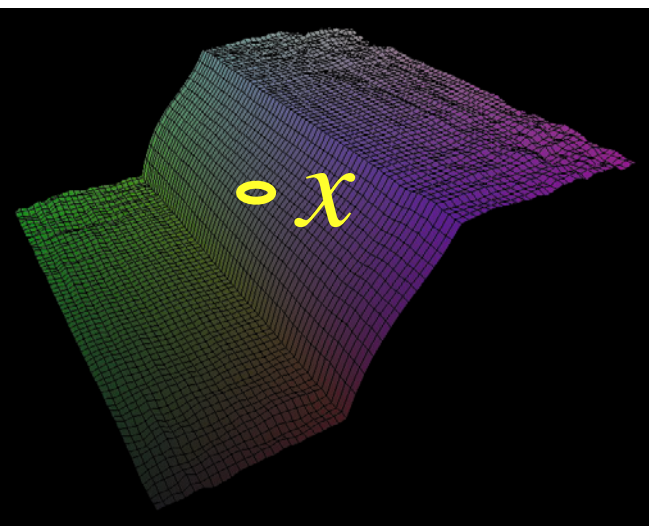


input

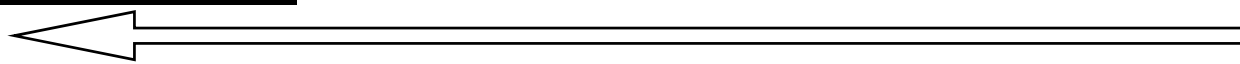
Gaussian filter as weighted average

- Weight of ξ depends on distance to \mathbf{x}

$$J(x) = \sum_{\xi} f(x, \xi) I(\xi)$$



output

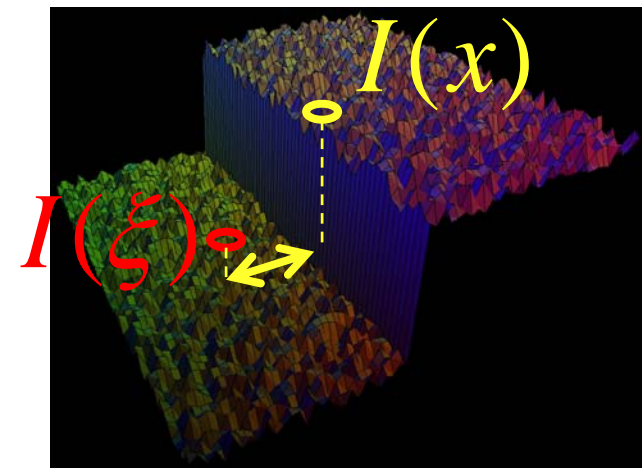
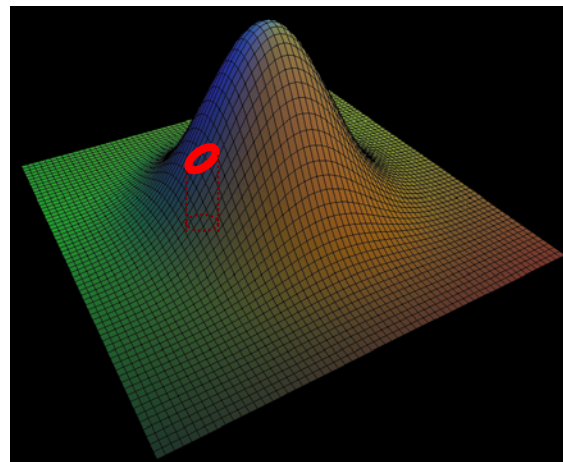
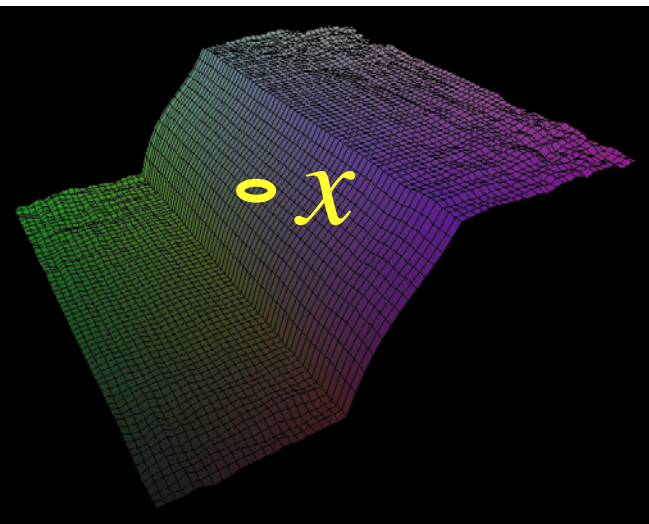


input

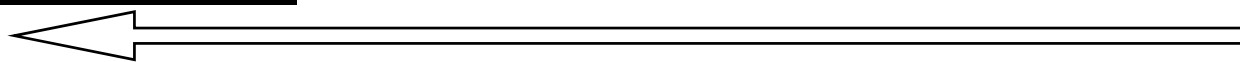
The problem of edges

- Here, $I(\xi)$ “pollutes” our estimate $J(x)$
- It is too different

$$J(x) = \sum_{\xi} f(x, \xi) \quad I(\xi)$$



output



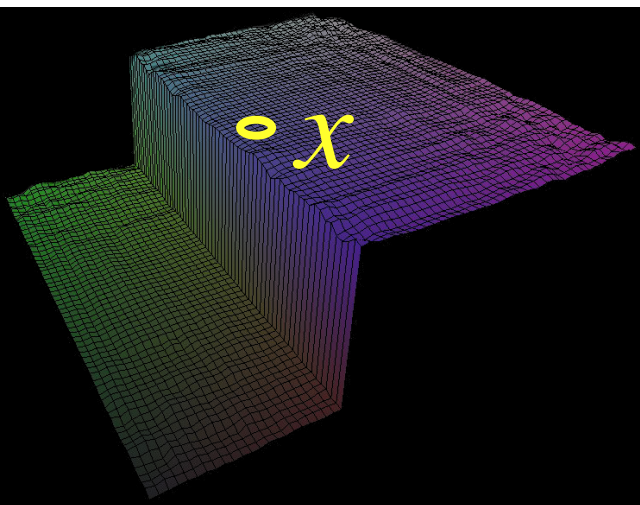
input

Principle of Bilateral filtering

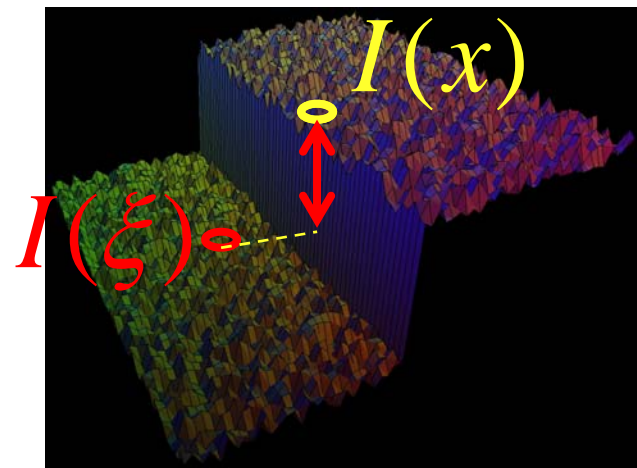
[Tomasi and Manduchi 1998]

- Penalty **g** on the intensity difference

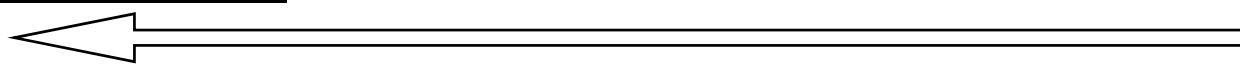
$$J(x) = \frac{1}{k(x)} \sum_{\xi} f(x, \xi) \quad g(I(\xi) - I(x)) \quad I(\xi)$$



output



input

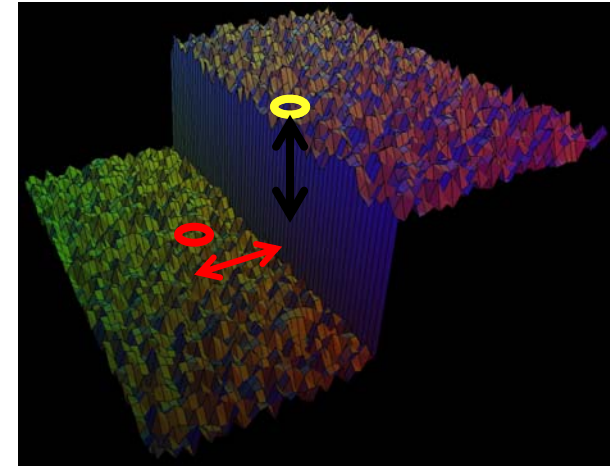
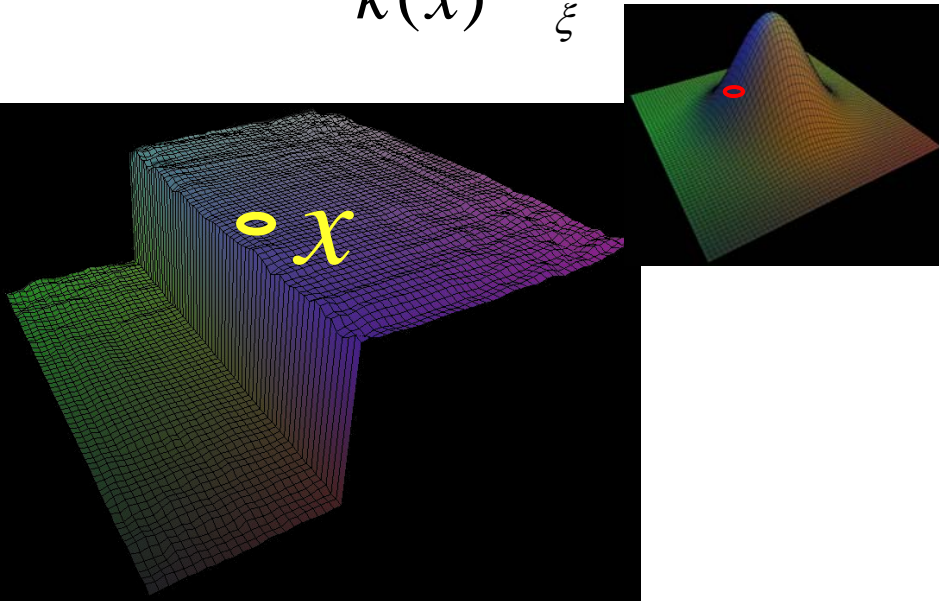


Bilateral filtering

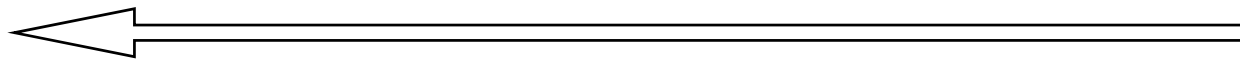
[Tomasi and Manduchi 1998]

- **Spatial Gaussian f**

$$J(x) = \frac{1}{k(x)} \sum_{\xi} f(x, \xi) \quad g(I(\xi) - I(x)) \quad I(\xi)$$



output



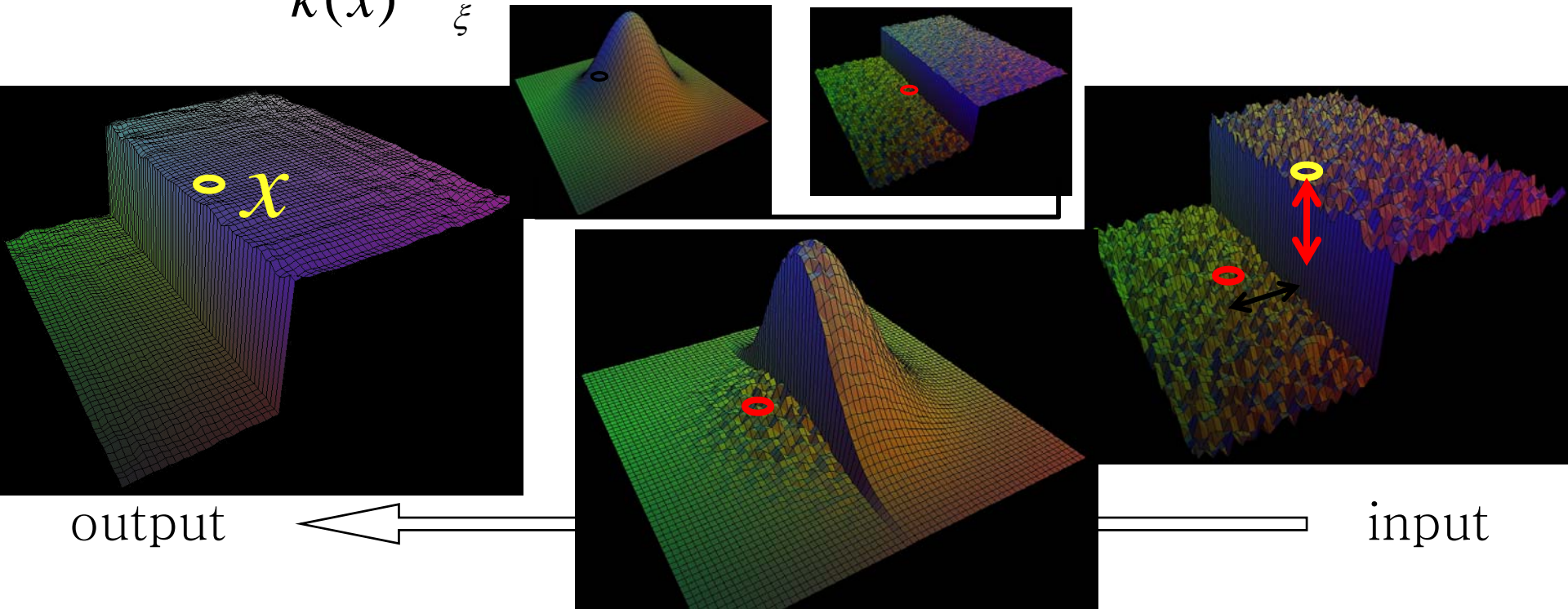
input

Bilateral filtering

[Tomasi and Manduchi 1998]

- **Spatial Gaussian f**
- **Gaussian g on the intensity difference**

$$J(x) = \frac{1}{k(x)} \sum_{\xi} f(x, \xi) g(I(\xi) - I(x)) I(\xi)$$

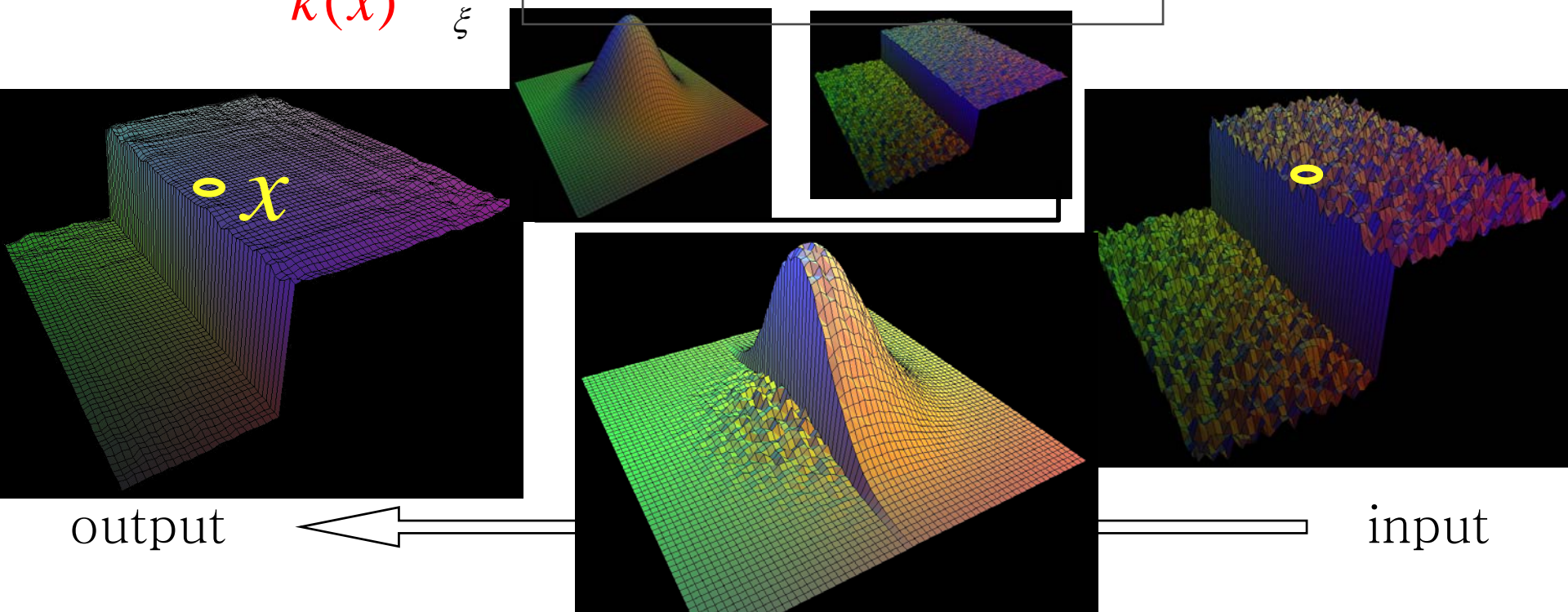


Normalization factor

[Tomasi and Manduchi 1998]

- $$\mathbf{k}(\mathbf{x}) = \sum_{\xi} f(x, \xi) \quad g(I(\xi) - I(x))$$

$$J(x) = \frac{1}{k(x)} \sum_{\xi} f(x, \xi) \quad g(I(\xi) - I(x)) \quad I(\xi)$$

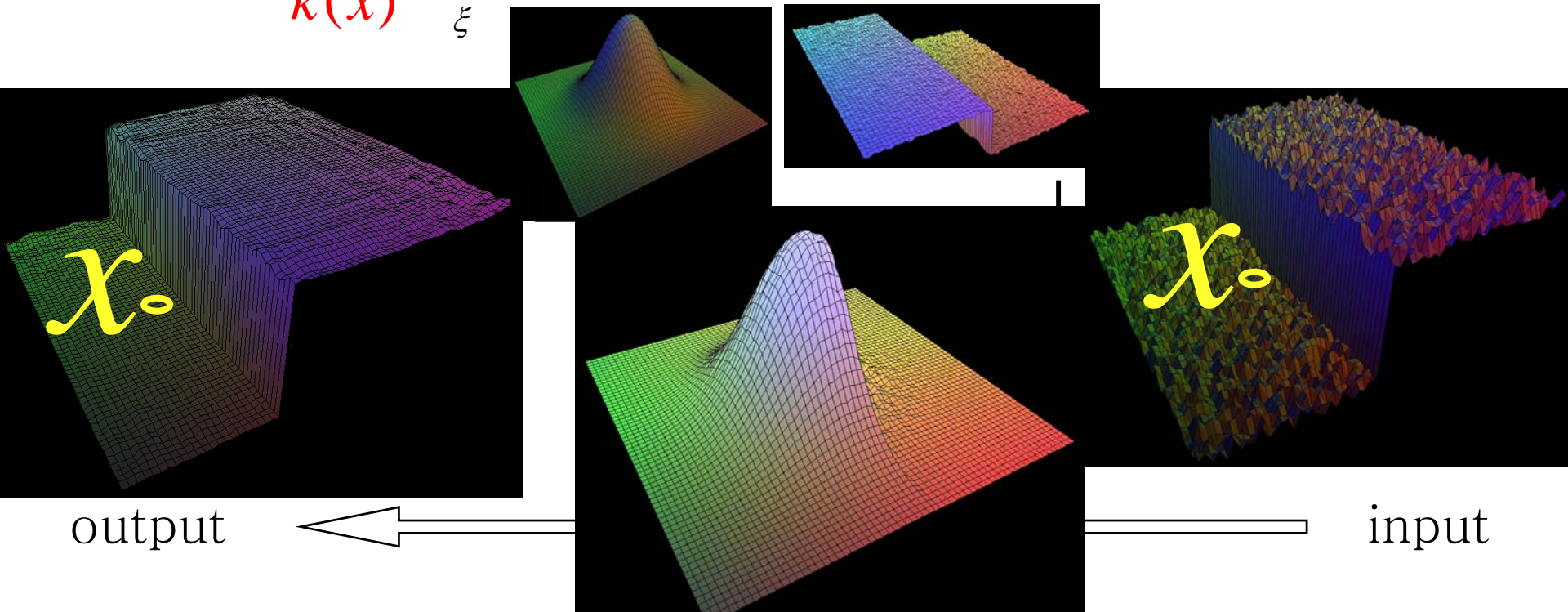


Bilateral filtering is non-linear

[Tomasi and Manduchi 1998]

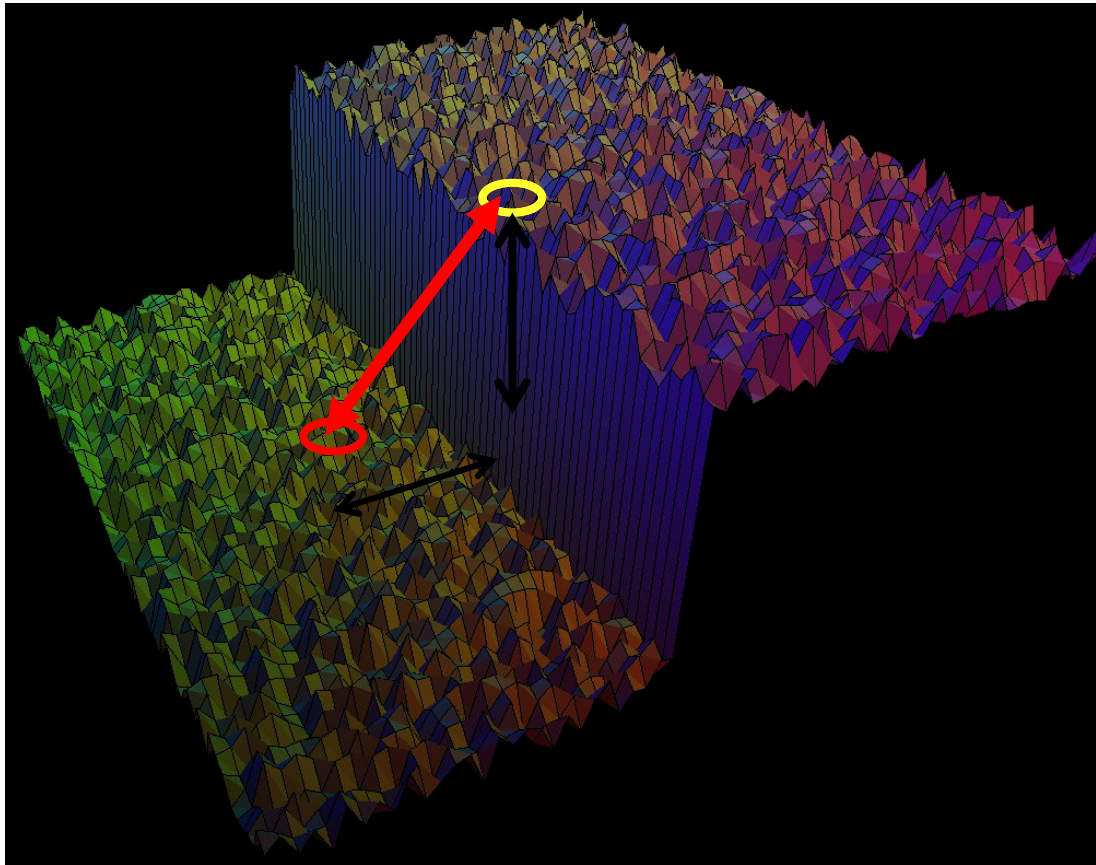
- The weights are different for each output pixel

$$J(x) = \frac{1}{k(x)} \sum_{\xi} f(x, \xi) \quad g(I(\xi) - I(x)) \quad I(\xi)$$



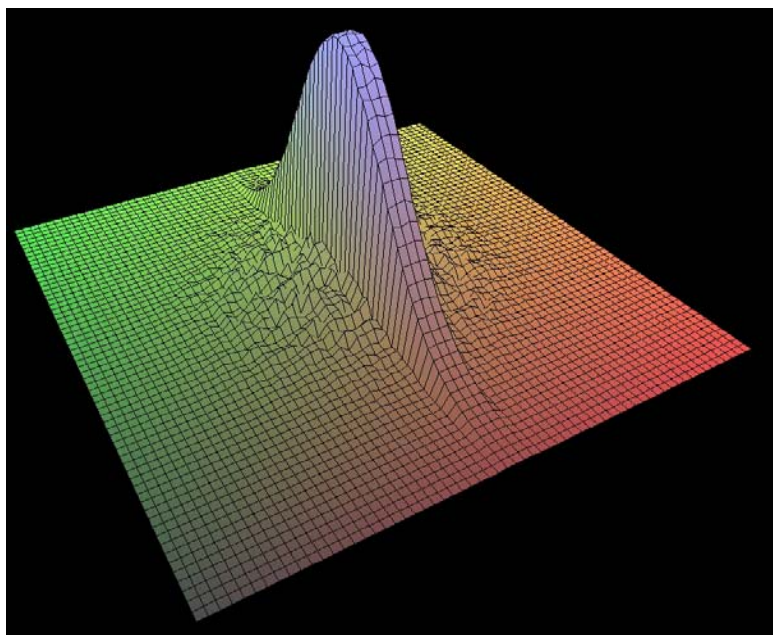
Other view

- The bilateral filter uses the 3D distance

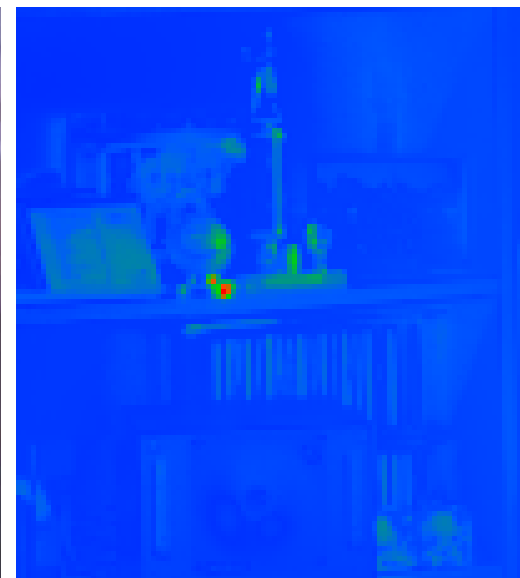
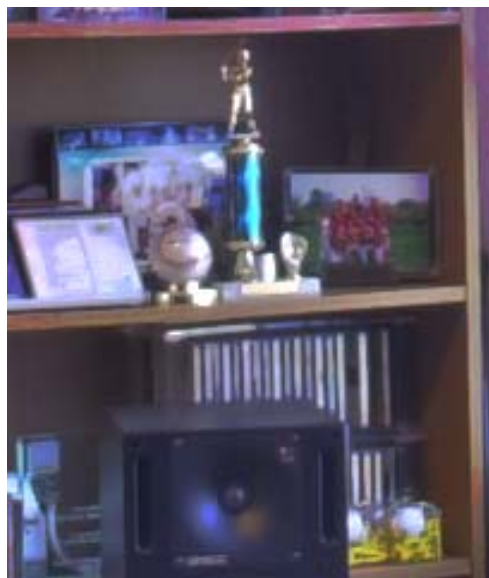


Handling uncertainty

- Sometimes, not enough “similar” pixels
- Happens for specular highlights
- Can be detected using normalization $k(x)$
- Simple fix (average with output of neighbors)



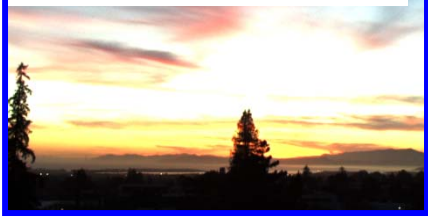
Weights with high uncertainty



Uncertainty

Contrast reduction

Input HDR image



Contrast
too high!

Contrast reduction

Input HDR image



Intensity



Color

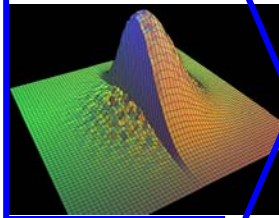


Contrast reduction

Input HDR image



Intensity

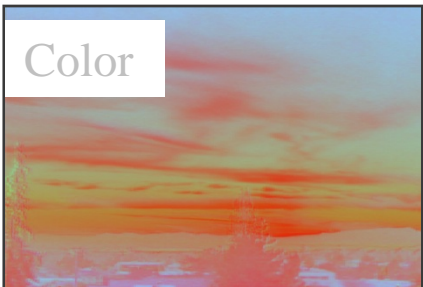


Large scale



Fast
Bilateral
Filter

Color

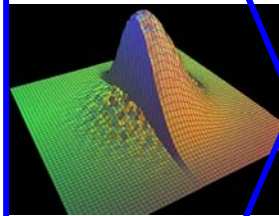


Contrast reduction

Input HDR image



Intensity



Fast
Bilateral
Filter

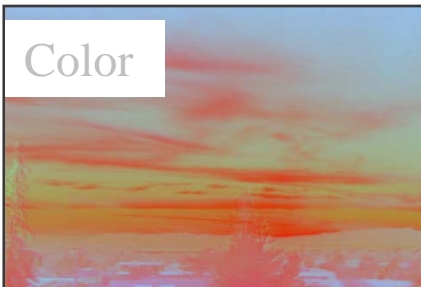
Large scale



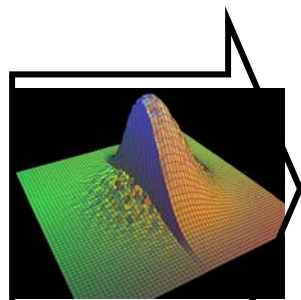
Detail



Color



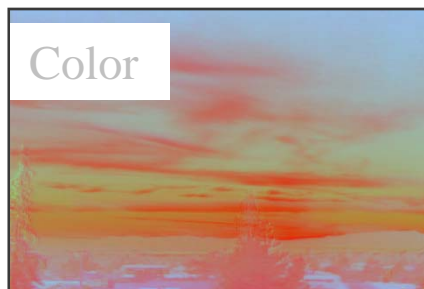
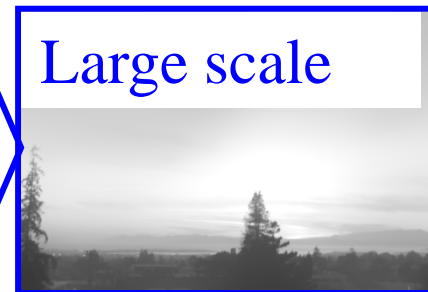
Contrast reduction



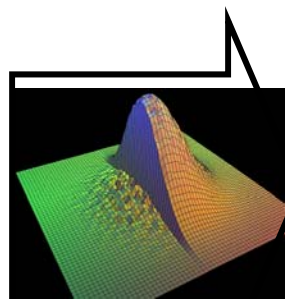
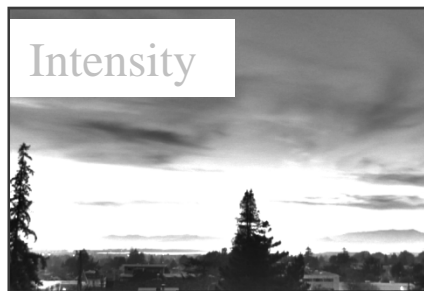
Fast
Bilateral
Filter



Reduce
contrast



Contrast reduction

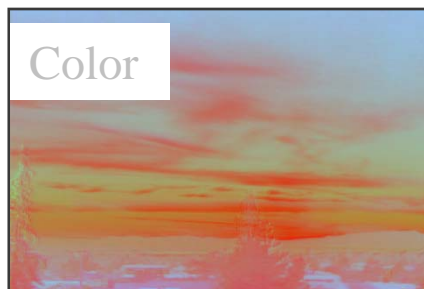
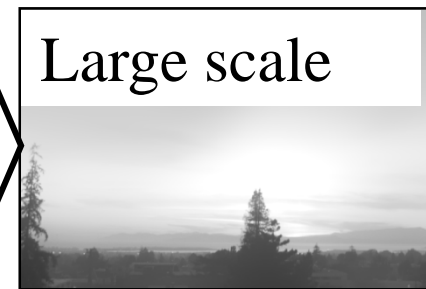


Fast
Bilateral
Filter

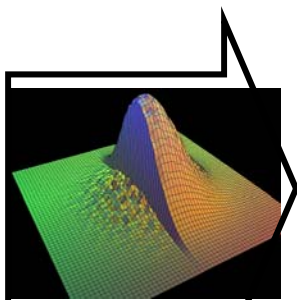
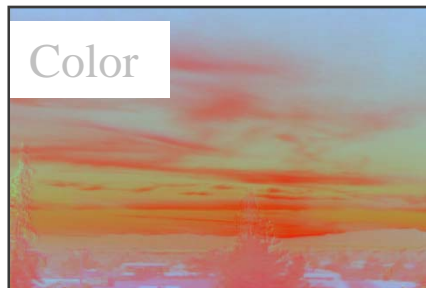


Reduce
contrast

Preserve!



Contrast reduction

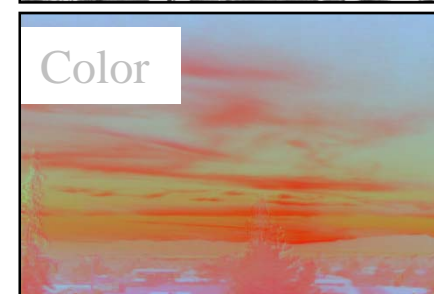
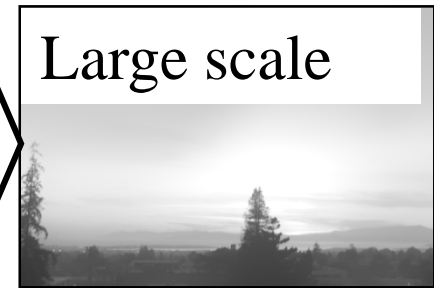


Fast
Bilateral
Filter



Reduce
contrast

Preserve!

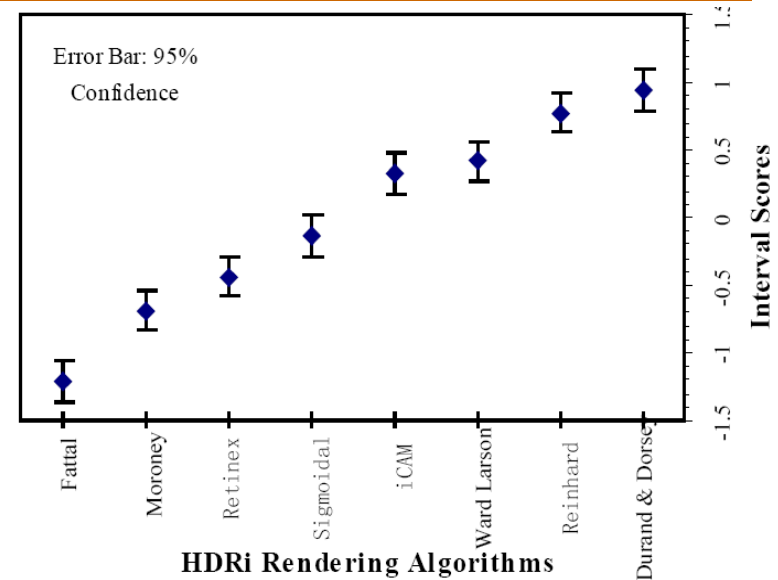


Reduction

- **To reduce contrast of base layer**
 - scale in the log domain
 - ➔ γ exponent in linear space
- **Set a target range: \log_{10} (5)**
- **Compute range in the base (log) layer: (max-min)**
- **Deduce γ using an elaborate operation known as *division***
- **You finally need to normalize so that the biggest value in the (linear) base is 1 (0 in log):**
 - Offset the compressed based by its max

Tone mapping evaluation

- **Recent work has performed user experiments to evaluate competing tone mapping operators**
 - Ledda et al. 2005
<http://www.cs.bris.ac.uk/Publications/Papers/2000255.pdf>
 - Kuang et al. 2004
<http://www.cis.rit.edu/fairchild/PDFs/PRO22.pdf>
- **Interestingly, the former concludes my method is the worst, the latter that my method is the best!**
 - They choose to test a different criterion: fidelity vs. preference
- **More importantly, they focus on algorithm and ignore parameters**



HDRi Rendering Algorithms

From Kuang et al.

	1st	2nd	3rd	4th	5th	6th
Scene 1	P	B	A	H	I	L
Scene 2	I	P	H	A	B	L
Scene 3	P	I	A	H	L	B
Scene 4	P	L	I	A	H	B
Scene 5	I	H	A	P	L	B
Scene 6	I	H	A	P	L	B
Scene 7	I	A	P	H	B	L
Scene 8	I	P	A	H	L	B
Scene 9	P	A	L	H	B	I

Adapted from Ledda et al.

Other tone mapping references

- **J. DiCarlo and B. Wandell, Rendering High Dynamic Range Images**
http://www-isl.stanford.edu/%7Eabbas/group/papers_and_pub/spie00_jeff.pdf
- **Choudhury, P., Tumblin, J., "The Trilateral Filter for High Contrast Images and Meshes"**. <http://www.cs.northwestern.edu/~jet/publications.html>
- **Tumblin, J., Turk, G., "Low Curvature Image Simplifiers (LCIS): A Boundary Hierarchy for Detail-Preserving Contrast Reduction."**
<http://www.cs.northwestern.edu/~jet/publications.html>
- **Tumblin, J., "Three Methods For Detail-Preserving Contrast Reduction For Displayed Images"** <http://www.cs.northwestern.edu/~jet/publications.html>
- **Photographic Tone Reproduction for Digital Images**
Erik Reinhard, Mike Stark, Peter Shirley and Jim Ferwerda
<http://www.cs.utah.edu/%7Eereinhard/cdrom/>
- **Ashikhmin, M. "A Tone Mapping Algorithm for High Contrast Images"** <http://www.cs.sunysb.edu/~ash/tm.pdf>
- **Retinex at Nasa** <http://dragon.larc.nasa.gov/retinex/background/retpubs.html>
- **Gradient Domain High Dynamic Range Compression** Raanan Fattal, Dani Lischinski, Michael Werman <http://www.cs.huji.ac.il/~danix/hdr/>
- **Li et al. : Wavelets and activity maps** http://web.mit.edu/yzli/www/hdr_companing.htm

Tone mapping code

- <http://www.mpi-sb.mpg.de/resources/pfstools/>
- <http://scanline.ca/exrtools/>
- <http://www.cs.utah.edu/~reinhard/cdrom/source.html>
- <http://www.cis.rit.edu/mcsl/icam/hdr/>

Next week

- Easter break!

